Supplement to "Earnings inequality and dynamics in the presence of informality: The case of Brazil"

(Quantitative Economics, Vol. 13, No. 4, November 2022, 1405–1446)

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We provide additional summary statistics in Appendix A. We present additional figures for Brazil's formal sector in Appendix B. We present additional figures for Brazil's informal sector in Appendix C. We discuss the role of multiple job holdings in Appendix D. We demonstrate the limited role of demographics in explaining the decline of the variance of residual log earnings changes in Appendix E.

APPENDIX A: ADDITIONAL SUMMARY STATISTICS

Table A.1. Cross-sectional summary statistics, overall.

| Year | Obs. | Mean | Std. dev. | P1 | P5 | P10 | P25 | P50 | P75 | P90 | P95 | P99 | P99.9 | P99.99 |
|------|------|--------|-----------|-----|------|------|------|--------|--------|--------|--------|---------|---------|---------|
| 1985 | 15.7 | 19,852 | 26,915 | 585 | 1755 | 3121 | 5881 | 11,105 | 22,696 | 44,737 | 67,256 | 134,110 | 255,402 | 425,948 |
| 1986 | 16.9 | 20,627 | 26,716 | 635 | 1751 | 3038 | 5932 | 11,865 | 24,215 | 47,043 | 69,680 | 134,984 | 224,955 | 387,154 |
| 1987 | 17.6 | 18,824 | 27,220 | 429 | 1364 | 2496 | 5009 | 10,438 | 21,323 | 42,172 | 64,080 | 134,699 | 290,922 | 403,407 |
| 1988 | 18.6 | 18,859 | 27,307 | 291 | 1148 | 2430 | 4910 | 10,045 | 21,266 | 42,977 | 66,632 | 137,842 | 256,362 | 396,512 |
| 1989 | 19.3 | 18,591 | 27,174 | 231 | 935 | 2319 | 4835 | 9839 | 20,902 | 41,922 | 65,923 | 139,556 | 254,659 | 387,672 |
| 1990 | 19.7 | 15,268 | 21,970 | 232 | 962 | 1873 | 3766 | 8078 | 17,521 | 34,687 | 54,200 | 112,631 | 199,526 | 297,985 |
| 1991 | 19.5 | 14,533 | 20,786 | 319 | 1021 | 1915 | 3861 | 7833 | 16,536 | 32,834 | 51,001 | 104,857 | 192,177 | 315,036 |
| 1992 | 19.4 | 14,399 | 20,297 | 202 | 826 | 1804 | 3936 | 7844 | 16,229 | 33,058 | 50,913 | 101,826 | 189,134 | 277,698 |
| 1993 | 20.1 | 15,728 | 23,111 | 162 | 766 | 1899 | 4178 | 8239 | 17,393 | 36,211 | 56,422 | 117,313 | 217,039 | 324,278 |
| 1994 | 20.7 | 16,524 | 23,245 | 244 | 1046 | 2074 | 4260 | 8671 | 18,903 | 38,908 | 58,775 | 117,161 | 211,849 | 305,908 |
| 1995 | 21.8 | 19,214 | 27,671 | 502 | 1345 | 2336 | 4723 | 9921 | 21,786 | 45,038 | 69,210 | 141,114 | 253,044 | 348,350 |
| 1996 | 21.9 | 19,335 | 27,785 | 574 | 1457 | 2468 | 4991 | 10,250 | 21,771 | 44,745 | 68,389 | 141,832 | 262,035 | 373,896 |
| 1997 | 22.3 | 19,434 | 28,048 | 594 | 1518 | 2552 | 5099 | 10,342 | 21,726 | 44,565 | 68,732 | 143,569 | 264,084 | 384,921 |
| 1998 | 22.9 | 19,869 | 29,077 | 623 | 1581 | 2687 | 5301 | 10,594 | 22,129 | 44,593 | 69,648 | 148,988 | 282,161 | 412,739 |
| 1999 | 23.1 | 19,153 | 28,001 | 613 | 1544 | 2628 | 5230 | 10,257 | 21,224 | 42,486 | 67,007 | 144,740 | 271,705 | 392,265 |
| 2000 | 23.7 | 19,013 | 28,187 | 608 | 1516 | 2613 | 5214 | 10,116 | 20,932 | 42,019 | 66,764 | 146,056 | 276,394 | 393,854 |
| 2001 | 25.4 | 19,133 | 29,659 | 619 | 1543 | 2648 | 5268 | 9954 | 20,582 | 42,124 | 66,775 | 151,038 | 311,010 | 464,091 |
| 2002 | 26.4 | 18,756 | 30,505 | 623 | 1551 | 2660 | 5292 | 9708 | 20,055 | 41,195 | 65,011 | 147,759 | 313,361 | 474,376 |
| 2003 | 27.4 | 17,699 | 27,930 | 596 | 1527 | 2596 | | 9236 | 18,791 | 38,405 | 60,946 | 138,945 | 306,786 | 475,542 |
| 2004 | 28.8 | 18,017 | 28,201 | 623 | 1600 | 2730 | 5386 | 9543 | 19,086 | 39,022 | 61,793 | 140,291 | 305,658 | 486,266 |
| 2005 | 30.5 | 17,974 | 28,196 | 628 | 1614 | 2752 | 5533 | 9554 | 18,908 | 38,617 | 61,227 | 140,834 | 304,485 | 489,218 |
| 2006 | 32.3 | 18,645 | 29,425 | 664 | 1736 | 2955 | 5992 | 9892 | 19,412 | 39,774 | 62,802 | 145,559 | 335,661 | 522,767 |
| | | 18,996 | | | | 3055 | | | | | | | 339,696 | |
| | | 19,464 | * | | | | | | | | | | 339,068 | |
| | | 19,866 | , | | | | | | | | | | 333,382 | |
| | | 20,392 | 31,395 | | | | | | | | | | 339,306 | |
| | | 20,773 | 31,431 | 804 | 2081 | | | | | | | | 333,256 | |
| | | 21,589 | 31,614 | | 2247 | | | | | | | | 326,983 | |
| | | 22,085 | 31,783 | | | | | | | | | | 328,978 | |
| | | 22,602 | 32,090 | | | | | | | | | | 331,021 | |
| | | 22,566 | 31,988 | | | 4242 | | | | | | | 336,925 | |
| | | 22,342 | 30,764 | | | 4363 | | | | | | | 317,613 | |
| | | 22,882 | * | | 2660 | 4498 | | | | | | | 317,728 | |
| 2018 | 42.5 | 22,641 | 30,825 | 985 | 2687 | 4534 | 8889 | 13,566 | 24,124 | 46,854 | 71,716 | 155,823 | 310,005 | 562,571 |

Note: Workers aged 25-55. Source: RAIS, 1985-2018.

Table A.2. Cross-sectional summary statistics, men only.

| Year | Obs. | Mean | Std. dev. | P1 | P5 | P10 | P25 | P50 | P75 | P90 | P95 | P99 | P99.9 | P99.99 |
|------|------|--------|-----------|------|------|------|------|--------|--------|--------|--------|---------|---------|---------|
| 1985 | 10.9 | 21,806 | 29,738 | 604 | 1810 | 3261 | 6253 | 12,064 | 24,781 | 49,741 | 75,852 | 147,933 | 276,815 | 452,345 |
| 1986 | 11.5 | 22,594 | 29,240 | 694 | 1908 | 3338 | 6467 | 12,983 | 26,291 | 51,689 | 78,045 | 147,480 | 240,500 | 411,612 |
| 1987 | 11.9 | 20,694 | 29,192 | 478 | 1483 | 2753 | 5566 | 11,583 | 23,246 | 46,531 | 72,300 | 147,748 | 279,048 | 407,918 |
| 1988 | 12.5 | 20,678 | 29,802 | 310 | 1199 | 2529 | 5287 | 11,099 | 23,169 | 47,432 | 73,964 | 151,087 | 273,212 | 414,375 |
| 1989 | 12.9 | 20,447 | 29,666 | 242 | 954 | 2390 | 5206 | 10,947 | 22,825 | 46,691 | 73,473 | 152,709 | 269,575 | 397,090 |
| 1990 | 13.0 | 16,529 | 23,716 | 246 | 1002 | 1951 | 4039 | 8869 | 18,787 | 37,744 | 59,386 | 121,774 | 210,552 | 315,132 |
| 1991 | 12.9 | 15,800 | 22,601 | 335 | 1052 | 1983 | 4109 | 8597 | 17,775 | 35,778 | 56,068 | 114,615 | 202,884 | 340,364 |
| 1992 | 12.7 | 15,789 | 22,315 | 208 | 821 | 1794 | 4111 | 8613 | 17,770 | 36,652 | 56,589 | 112,009 | 200,857 | 298,910 |
| 1993 | 13.1 | 17,225 | 25,278 | 166 | 747 | 1851 | 4356 | 9037 | 18,915 | 40,227 | 62,608 | 128,325 | 231,322 | 349,415 |
| 1994 | 13.4 | 17,821 | 25,239 | 248 | 1050 | 2098 | 4470 | 9391 | 20,162 | 41,854 | 64,054 | 128,022 | 225,410 | 324,779 |
| 1995 | 14.0 | 20,857 | 29,942 | 524 | 1399 | 2442 | 5045 | 10,859 | 23,422 | 48,993 | 75,825 | 153,967 | 265,982 | 369,637 |
| 1996 | 13.9 | 20,897 | 30,184 | 599 | 1512 | 2569 | 5301 | 11,112 | 23,125 | 48,491 | 75,210 | 154,839 | 276,879 | 392,875 |
| 1997 | 14.1 | 20,874 | 30,399 | 612 | 1533 | 2617 | 5362 | 11,132 | 22,875 | 47,940 | 75,304 | 156,928 | 279,669 | 402,947 |
| 1998 | 14.4 | 21,114 | 31,347 | 638 | 1590 | 2702 | 5548 | 11,307 | 22,916 | 47,183 | 75,734 | 162,362 | 298,428 | 432,973 |
| 1999 | 14.3 | 20,281 | 30,187 | 628 | 1539 | 2616 | 5420 | 10,891 | 21,868 | 44,684 | 72,806 | 157,247 | 288,153 | 413,110 |
| 2000 | 14.7 | 19,991 | 30,046 | 628 | 1523 | 2615 | 5381 | 10,710 | 21,554 | 43,731 | 71,470 | 157,184 | 291,335 | 409,962 |
| 2001 | 15.7 | 20,302 | 32,017 | 629 | 1558 | 2671 | 5468 | 10,556 | 21,361 | 44,346 | 72,585 | 163,447 | 333,319 | 482,633 |
| 2002 | 16.2 | 19,775 | 33,302 | 654 | 1575 | 2676 | 5469 | 10,316 | 20,718 | 42,822 | 69,725 | 159,904 | 335,594 | 493,453 |
| 2003 | 16.7 | 18,711 | 30,140 | 628 | 1545 | 2606 | 5349 | 9876 | 19,464 | 40,006 | 65,655 | 151,336 | 331,293 | 499,499 |
| 2004 | 17.5 | 19,079 | 30,457 | 663 | 1624 | 2768 | 5575 | 10,110 | 19,842 | 40,676 | 66,423 | 153,033 | 331,317 | 511,021 |
| 2005 | 18.4 | 19,048 | 30,436 | 668 | 1671 | 2825 | 5721 | 10,205 | 19,709 | 40,218 | 65,629 | 153,618 | 328,746 | 518,375 |
| 2006 | 19.4 | 19,689 | 31,636 | 712 | 1803 | 3042 | 6162 | 10,627 | 20,176 | 41,152 | 66,822 | 157,486 | 358,328 | 558,436 |
| 2007 | 20.5 | 20,062 | 31,930 | 740 | 1883 | 3167 | 6441 | 10,916 | 20,527 | 41,898 | 67,361 | 159,765 | 357,695 | 568,516 |
| 2008 | 21.8 | 20,638 | 32,709 | 804 | 2031 | 3363 | 6695 | 11,283 | 21,149 | 42,798 | 68,702 | 165,123 | 359,067 | 584,843 |
| 2009 | 22.4 | 21,001 | 33,154 | 785 | 2000 | 3371 | 6938 | 11,570 | 21,433 | 43,537 | 70,143 | 168,102 | 355,285 | 596,351 |
| 2010 | 23.7 | 21,662 | 33,744 | 867 | 2218 | 3657 | 7362 | 12,105 | 22,174 | 44,496 | 71,921 | 169,397 | 362,153 | 618,336 |
| 2011 | 24.7 | 22,178 | 33,898 | 902 | 2317 | 3825 | 7579 | 12,608 | 22,949 | 45,473 | 72,672 | 169,992 | 357,621 | 623,517 |
| 2012 | 25.3 | 23,064 | 34,277 | 973 | 2503 | 4154 | 8219 | 13,442 | 24,119 | 47,239 | 74,429 | 171,979 | 355,940 | 633,150 |
| 2013 | 25.8 | 23,691 | 34,468 | 999 | 2582 | 4257 | 8435 | 14,033 | 24,991 | 48,562 | 75,997 | 173,752 | 359,881 | 642,189 |
| 2014 | 26.0 | 24,235 | 34,812 | 1042 | 2652 | 4420 | 8709 | 14,489 | 25,652 | 49,641 | 77,273 | 176,476 | 362,136 | 646,920 |
| 2015 | 25.3 | 24,077 | 34,642 | 1014 | 2641 | 4452 | 8773 | 14,463 | 25,291 | 49,160 | 76,822 | 175,220 | 364,824 | 643,974 |
| 2016 | 24.1 | 23,693 | 33,301 | 1021 | 2679 | 4478 | 8929 | 14,448 | 25,000 | 48,133 | 75,243 | 168,912 | 344,804 | 623,699 |
| 2017 | 23.6 | 24,233 | 33,968 | 1037 | 2743 | 4595 | 9190 | 14,788 | 25,503 | 49,042 | 76,947 | 172,357 | 346,970 | 631,279 |
| 2018 | 23.7 | 23,919 | 33,340 | 1053 | 2763 | 4650 | 9190 | 14,606 | 25,136 | 48,419 | 75,901 | 168,979 | 340,037 | 615,497 |
| | | | | | | | | | | | | | | |

Note: Workers aged 25–55. Source: RAIS, 1985–2018.

Table A.3. Cross-sectional summary statistics, women only.

| Year | Obs. | Mean | Std. dev. | P1 | P5 | P10 | P25 | P50 | P75 | P90 | P95 | P99 | P99.9 | P99.99 |
|------|------|--------|-----------|-----|------|------|------|--------|--------|--------|--------|---------|---------|---------|
| 1985 | 4.8 | 15,463 | 18,364 | 533 | 1661 | 2857 | 5378 | 9299 | 18,347 | 35,186 | 49,613 | 89,725 | 162,360 | 292,297 |
| 1986 | 5.4 | 16,417 | 19,630 | 546 | 1503 | 2547 | 5203 | 9744 | 19,903 | 38,414 | 53,682 | 95,500 | 170,577 | 266,223 |
| 1987 | 5.7 | 14,943 | 22,087 | 356 | 1142 | 2103 | 4320 | 8419 | 17,244 | 34,083 | 48,978 | 95,853 | 349,114 | 390,751 |
| 1988 | 6.1 | 15,117 | 20,772 | 257 | 1049 | 2228 | 4415 | 8304 | 17,418 | 34,025 | 51,686 | 107,098 | 189,608 | 326,275 |
| 1989 | 6.4 | 14,846 | 20,777 | 211 | 896 | 2203 | 4411 | 8027 | 17,087 | 33,021 | 49,989 | 106,495 | 194,909 | 343,763 |
| 1990 | 6.7 | 12,811 | 17,837 | 208 | 896 | 1740 | 3422 | 6714 | 15,037 | 29,584 | 43,748 | 90,607 | 166,149 | 246,986 |
| 1991 | 6.7 | 12,095 | 16,477 | 295 | 961 | 1792 | 3534 | 6540 | 14,030 | 27,533 | 41,404 | 82,045 | 155,255 | 233,028 |
| 1992 | 6.6 | 11,734 | 15,371 | 193 | 841 | 1825 | 3708 | 6617 | 13,605 | 26,583 | 39,789 | 75,928 | 143,422 | 217,458 |
| 1993 | 7.0 | 12,953 | 18,102 | 157 | 794 | 1976 | 3984 | 7028 | 14,575 | 28,827 | 44,341 | 92,373 | 170,239 | 253,249 |
| 1994 | 7.4 | 14,173 | 18,880 | 240 | 1042 | 2036 | 3981 | 7491 | 16,652 | 33,813 | 49,774 | 93,499 | 168,105 | 249,112 |
| 1995 | 7.9 | 16,297 | 22,808 | 473 | 1269 | 2166 | 4330 | 8455 | 18,752 | 38,458 | 57,993 | 112,305 | 214,995 | 300,946 |
| 1996 | 8.0 | 16,631 | 22,796 | 545 | 1378 | 2313 | 4630 | 8977 | 19,368 | 38,579 | 57,574 | 111,614 | 221,920 | 322,283 |
| 1997 | 8.2 | 16,970 | 23,283 | 566 | 1457 | 2458 | 4757 | 9182 | 19,679 | 39,252 | 58,677 | 115,559 | 222,966 | 331,703 |
| 1998 | 8.5 | 17,766 | 24,633 | 596 | 1557 | 2660 | 5012 | 9538 | 20,624 | 40,835 | 60,858 | 123,556 | 238,938 | 355,660 |
| 1999 | 8.7 | 17,303 | 23,873 | 594 | 1545 | 2648 | 5003 | 9341 | 19,935 | 39,492 | 58,859 | 120,402 | 232,289 | 338,864 |
| 2000 | 9.0 | 17,418 | 24,775 | 584 | 1503 | 2611 | 4967 | 9221 | 19,764 | 39,607 | 59,878 | 124,658 | 244,296 | 349,034 |
| 2001 | 9.7 | 17,251 | 25,295 | 579 | 1506 | 2606 | 5041 | 9014 | 19,182 | 39,091 | 58,914 | 125,432 | 266,031 | 397,658 |
| 2002 | 10.2 | 17,137 | 25,356 | 581 | 1520 | 2644 | 5069 | 8893 | 18,854 | 38,998 | 58,563 | 124,371 | 270,983 | 412,300 |
| 2003 | 10.7 | 16,118 | 23,989 | 560 | 1491 | 2576 | 5029 | 8458 | 17,511 | 36,165 | 54,682 | 116,725 | 261,294 | 415,282 |
| 2004 | 11.3 | 16,373 | 24,203 | 582 | 1552 | 2667 | 5197 | 8645 | 17,716 | 36,739 | 55,557 | 118,862 | 257,566 | 410,678 |
| 2005 | 12.1 | 16,334 | 24,289 | 580 | 1536 | 2648 | 5317 | 8604 | 17,408 | 36,366 | 55,475 | 119,903 | 261,916 | 399,578 |
| 2006 | 12.9 | 17,070 | 25,649 | 611 | 1641 | 2858 | 5822 | 8931 | 18,032 | 37,930 | 57,489 | 124,361 | 289,308 | 430,627 |
| 2007 | 13.7 | 17,407 | 26,145 | | 1658 | | | 9150 | 18,300 | 38,647 | 58,693 | 127,225 | 294,307 | 428,367 |
| | | 17,732 | 26,805 | | 1698 | | | 9323 | | | | | 302,464 | |
| | | 18,222 | 27,248 | | 1729 | | | 9675 | , | , | , | , | 300,453 | , |
| | | 18,580 | 27,601 | | 1805 | | | | , | , | , | , | 303,894 | , |
| | | 18,812 | 27,503 | | 1856 | | | , | | , | , | , | 298,549 | , |
| | | 19,580 | 27,449 | | 2010 | | | | | | | | 290,728 | |
| | | 19,942 | 27,655 | | | | | | | | | | 290,507 | |
| | | 20,460 | | | | | | | | | | | 290,801 | |
| | | 20,616 | , | | | | | , | , | , | , | , | 298,356 | , |
| | | 20,621 | 27,094 | | | | | , | , | , | , | , | 281,736 | , |
| | | 21,179 | , | | | | | | | | | | 280,049 | |
| 2018 | 18.9 | 21,038 | 27,260 | 923 | 2544 | 4376 | 8684 | 12,472 | 22,497 | 45,130 | 66,793 | 137,607 | 274,721 | 447,120 |

Note: Workers aged 25–55. Source: RAIS, 1985–2018.

APPENDIX B: ADDITIONAL FIGURES FOR BRAZIL'S FORMAL SECTOR

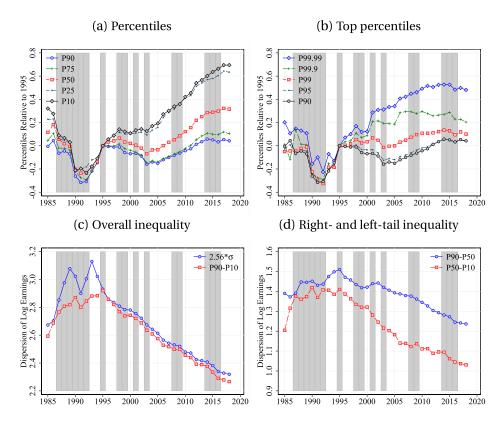


FIGURE B.1. Evolution of earnings percentiles, men and women pooled. Note: Workers aged 25-55. Source: RAIS, 1985-2018.



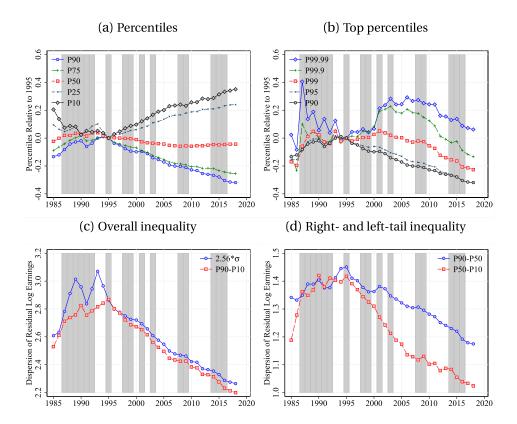


FIGURE B.2. Evolution of earnings percentiles, men and women pooled and controlling for age. *Note*: Workers aged 25–55. *Source*: RAIS, 1985–2018.

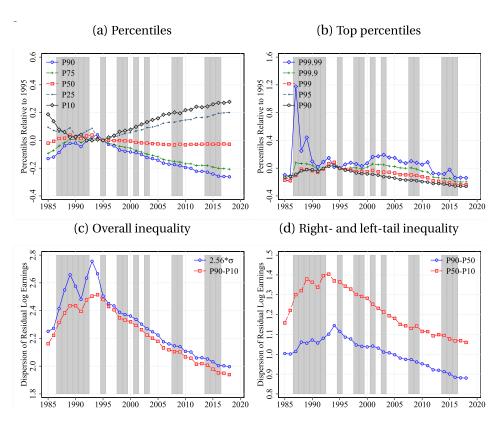


FIGURE B.3. Evolution of residual earnings percentiles, men and women pooled and controlling for age and education. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

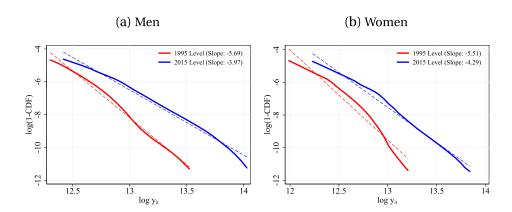


FIGURE B.4. Pareto tail within top 1%, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

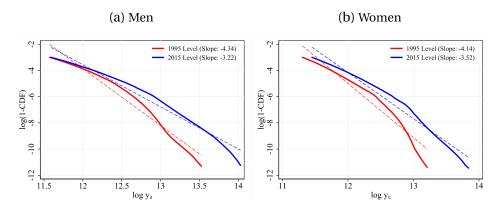


FIGURE B.5. Pareto tail within top 5%, by gender. *Note*: Workers aged 25–55. *Source*: RAIS, 1985–2018.

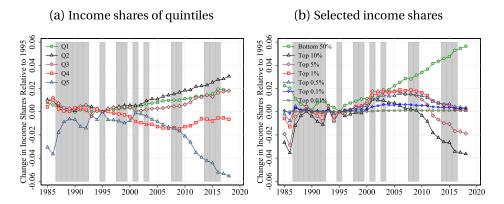


FIGURE B.6. Evolution of earnings shares, relative to 1995. *Note*: Workers aged 25–55. *Source*: RAIS, 1985–2018.

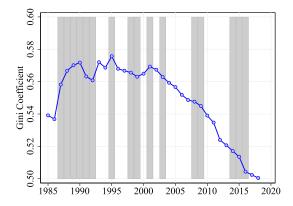


FIGURE B.7. Gini coefficient of earnings. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

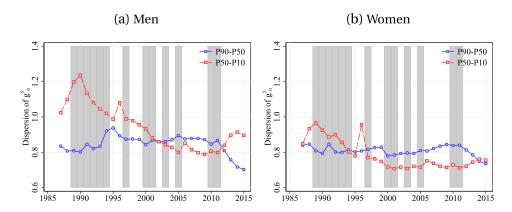


FIGURE B.8. Dispersion in 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

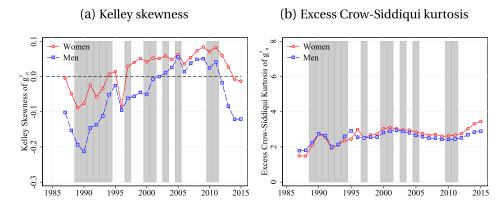


FIGURE B.9. Higher-order moments of the distribution of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

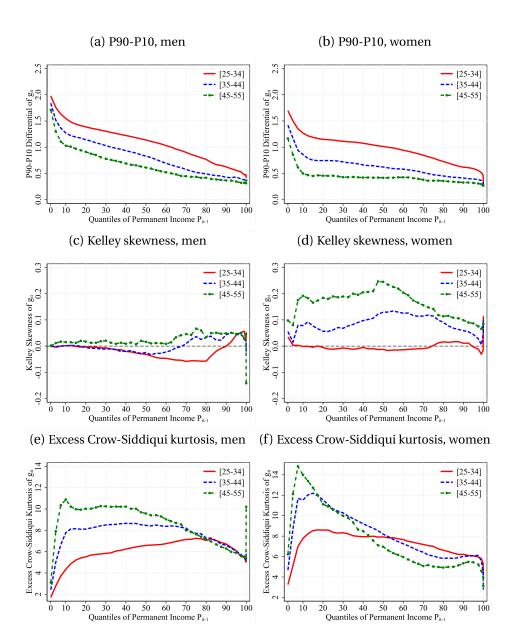


Figure B.10. Moments of the distribution of 5-year earnings changes, by gender. *Note*: Workers aged 25–55. *Source*: RAIS, 1999–2018.

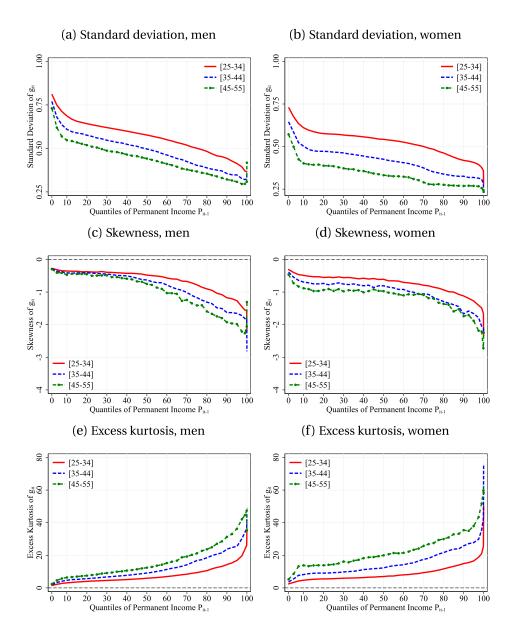


FIGURE B.11. Standardized moments of the distribution of 1-year earnings changes, by gender. *Note*: Workers aged 25–55. Skewness corresponds to the standardized third moment of the distribution. Excess kurtosis is defined as the standardized fourth moment of the distribution minus 3. *Source*: RAIS, 1999–2018.

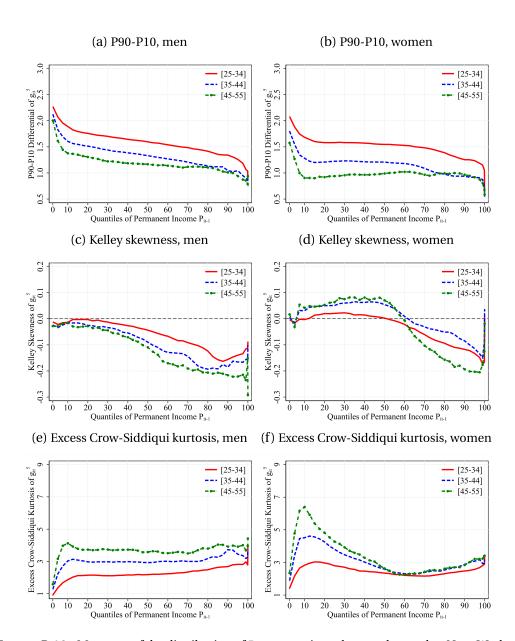


Figure B.12. Moments of the distribution of 5-year earnings changes, by gender. *Note*: Workers aged 25–55. *Source*: RAIS, 1999–2018.

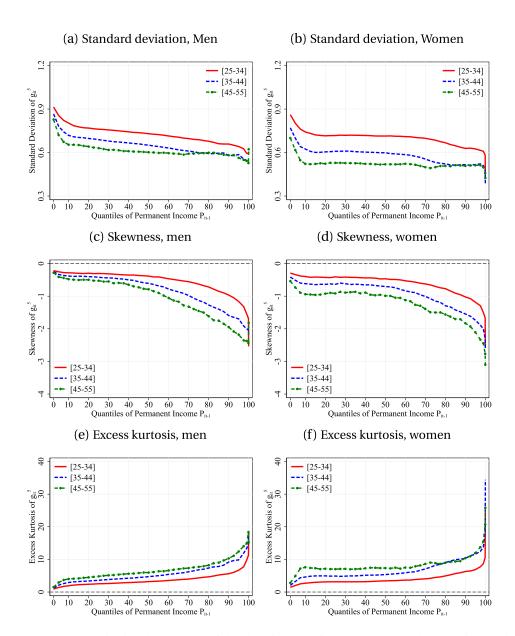


FIGURE B.13. Standardized moments of the distribution of 5-year earnings changes, by gender. *Note*: Workers aged 25–55. Skewness corresponds to the standardized third moment of the distribution. Excess kurtosis is defined as the standardized fourth moment of the distribution minus 3. *Source*: RAIS, 1999–2018.

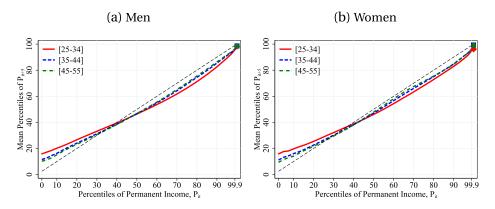


FIGURE B.14. Evolution of earnings mobility over the life cycle, by gender. *Note*: Workers aged 25–55. Colored markers denote the top 0.1% of permanent income P_{it} . *Source*: RAIS, 1985–2018.

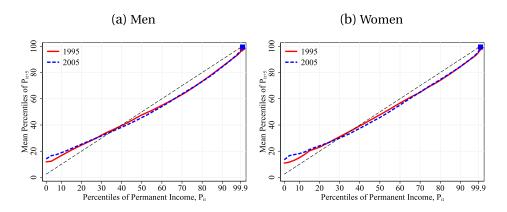


Figure B.15. Evolution of earnings mobility over time, by gender. *Note*: Workers aged 25–55. Colored markers denote the top 0.1% of permanent income P_{it} . *Source*: RAIS, 1985–2018.

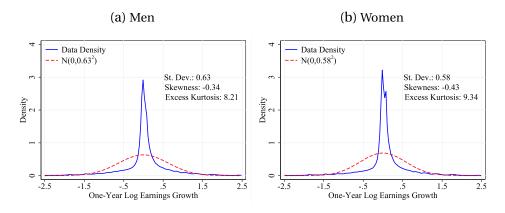


FIGURE B.16. Density of 1-year earnings changes, by gender. *Note*: Workers aged 25–55. *Source*: RAIS, 1985–2018.

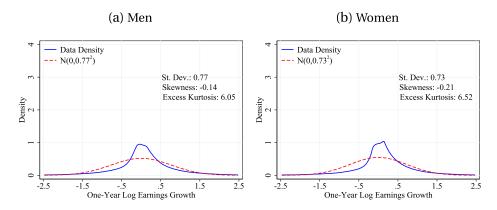


FIGURE B.17. Density of 5-year earnings changes, by gender. Note: Workers aged 25–55. Source: RAIS, 1985-2018.

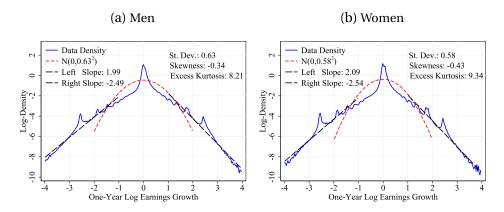


FIGURE B.18. Log density of 1-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

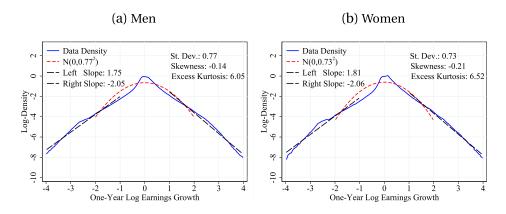


FIGURE B.19. Log density of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

APPENDIX C: ADDITIONAL FIGURES FOR BRAZIL'S INFORMAL SECTOR

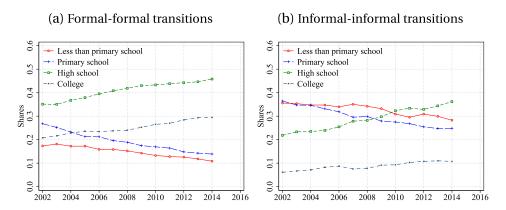


FIGURE C.1. Education shares, by origin and destination sector. *Note*: Workers aged 25–55. *Source*: PME, 2002–2015.

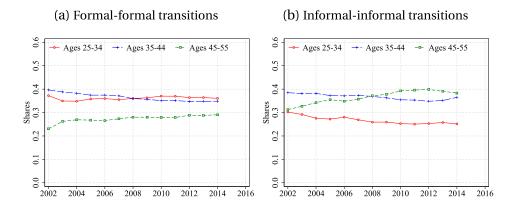


FIGURE C.2. Age group shares, by origin and destination sector. *Note*: Workers aged 25–55. *Source*: PME, 2002–2015.

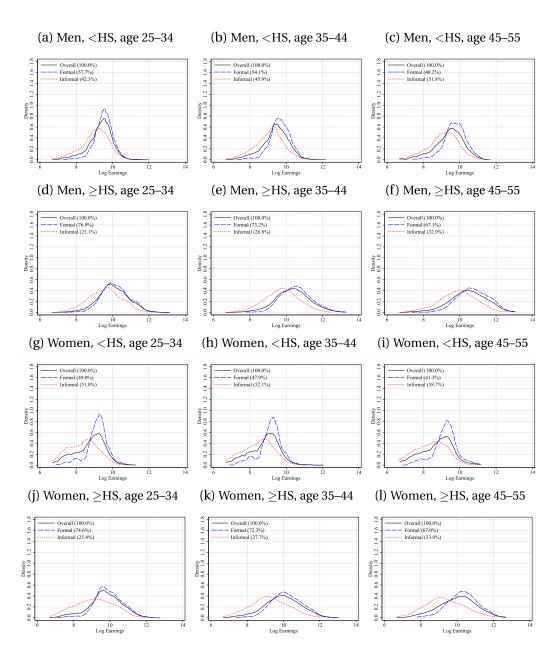


FIGURE C.3. Densities of log earnings, by sector and population subgroup in 2002. Note: Workers aged 25-55. Kernel densities of log earnings by worker group. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. Source: PME, 2002.

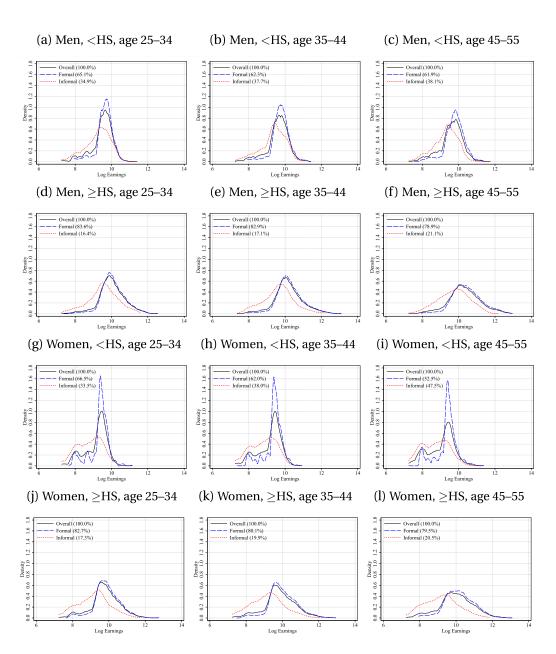


FIGURE C.4. Densities of log earnings, by sector and population subgroup in 2015. *Note*: Workers aged 25–55. Kernel densities of log earnings by worker group. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. *Source*: PME, 2015.

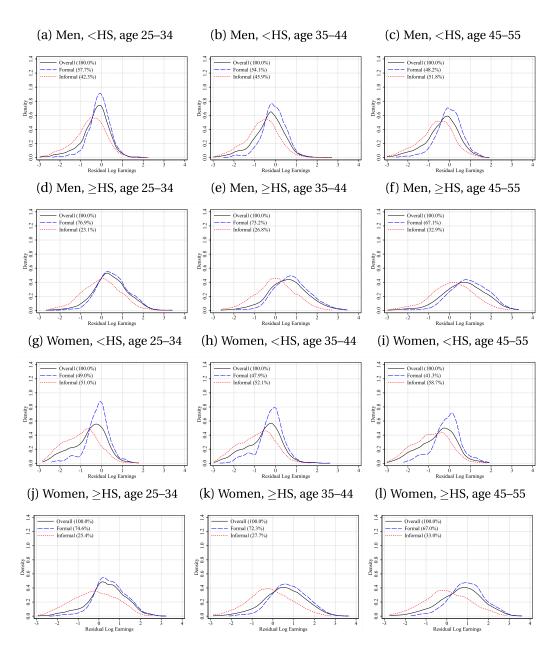


FIGURE C.5. Densities of residual log earnings, by sector and population subgroup in 2002. *Note*: Workers aged 25–55. Kernel densities of residual log earnings by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. *Source*: PME, 2002.

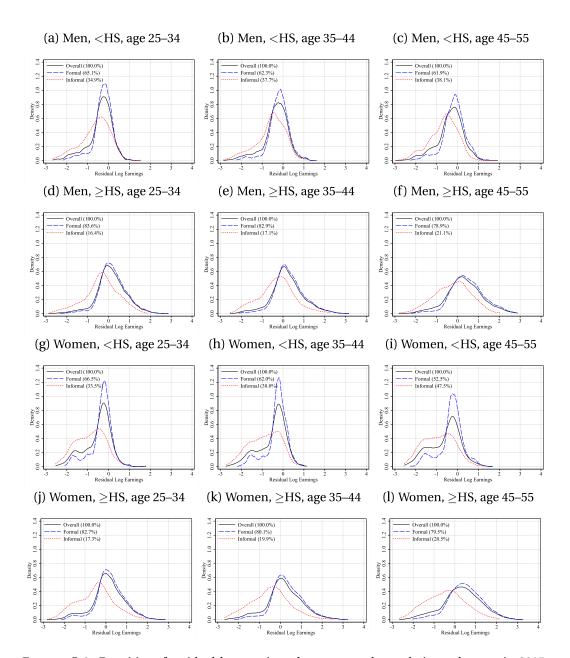


FIGURE C.6. Densities of residual log earnings, by sector and population subgroup in 2015. *Note*: Workers aged 25–55. Kernel densities of residual log earnings by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. *Source*: PME, 2015.

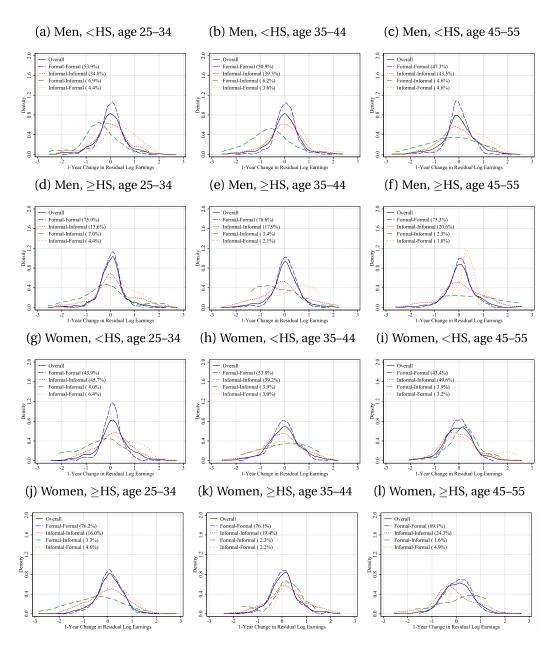


FIGURE C.7. Densities of 1-year residual log earnings changes, by transition type and population subgroup in 2002-2003. Note: This figure shows kernel densities of 1-year changes in residual log earnings for workers aged 25-55 by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines denote different combinations of a worker's current sector of employment and that in the next survey wave (e.g., "Formal-Informal" denotes current employment in the formal sector and employment in the informal sector in the next survey wave). Source: PME, 2002–2003.



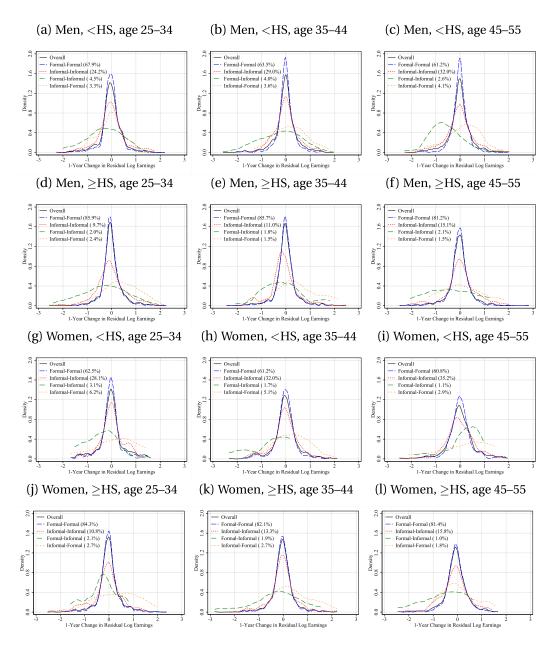


FIGURE C.8. Densities of 1-year residual log earnings changes, by transition type and population subgroup in 2014–2015. *Note*: This figure shows kernel densities of 1-year changes in residual log earnings for workers aged 25–55 by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines denote different combinations of a worker's current sector of employment and that in the next survey wave (e.g., "Formal-Informal" denotes current employment in the formal sector and employment in the informal sector in the next survey wave). *Source*: PME, 2014–2015.

| | P | anel A. Fo | rmal secto | or | Panel B. Informal sector | | | | | |
|--|---------|------------|------------|---------|--------------------------|---------|---------|---------|--|--|
| | 2002-04 | 2005-08 | 2009–11 | 2012–15 | 2002-04 | 2005-08 | 2009–11 | 2012–15 | | |
| Share with secondary job (%) | 2.8 | 2.9 | 2.7 | 2.3 | 2.1 | 2.3 | 2.1 | 2.2 | | |
| Mean weekly hours in main job | 42.8 | 42.5 | 42.3 | 42.0 | 41.8 | 41.6 | 41.0 | 40.3 | | |
| Mean weekly hours in secondary jobs | 17.5 | 17.2 | 15.0 | 16.7 | 22.2 | 21.8 | 20.2 | 21.6 | | |
| Share with SS contributions in secondary job | 51.2 | 52.2 | 54.4 | 59.1 | 25.0 | 23.5 | 25.7 | 30.9 | | |

Table D.1. Evolution of multiple-job-holding rates.

Note: Workers aged 25-55. Share of formal or informal employment with a secondary job. "Mean weekly hours in main job" is for the full sample population conditional on holding a job. "Mean weekly hours in secondary jobs" includes hours worked in all nonprimary (i.e., secondary, tertiary, etc.) jobs and is computed among the subpopulation of workers with more than one concurrent job. Source: PME, 2002-2015.

APPENDIX D: THE ROLE OF MULTIPLE JOB HOLDINGS

One may wonder whether the decrease in the informal employment share in Brazil is driven by changes in the prevalence of workers concurrently holding multiple jobs with a mix between formal and informal employment. To investigate this, Table D.1 summarizes the share of workers who hold multiple jobs in a month, broken down by whether the main job is in the formal sector (panel A) or informal sector (panel B). Holding multiple job is not particularly common in Brazil, with roughly 2% of employed workers holding multiple jobs. The fraction is modestly lower among informal sector workers. Among formal sector workers with a second job, roughly half of them contribute to social security in their second job (a proxy for the formality status of the second job). Moreover, the (un)importance of holding multiple jobs has remained roughly stable over time. Hence, the main margin of formalization is the extensive margin—workers switching entirely into the formal sector—as opposed to a declining prevalence of workers holding multiple jobs in both the informal and formal sector.

APPENDIX E: THE LIMITED ROLE OF DEMOGRAPHICS IN EXPLAINING THE DECLINE IN THE VARIANCE OF RESIDUAL LOG EARNINGS CHANGES

We here present a between-versus within-group decomposition similar to that in equation (4) of Section 4.1.4 of the main text (Engborn, Gonzaga, Moser, and Olivieri (2022)). Specifically, we decompose the overall variance of earnings changes for workers undergoing formal-formal and informal-informal sector transitions into between and within components by worker subgroups. Specifically, we focus on worker subgroups by four education groups. We restrict attention to the formal-formal and informal-informal worker groups because they constitute the great majority of Brazilian employment. Motivated by the fact that the within-education group component accounts for the great majority of changes in the volatility of earnings among formal-formal and informalinformal workers, we further consider a shift-share analysis of the within-education

2002 2002

2004

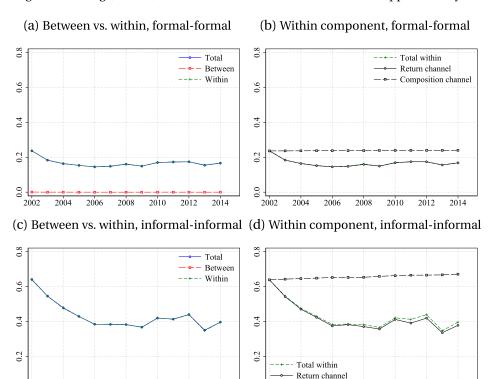


FIGURE E.1. The role of changes in educational attainment. *Note*: Workers aged 25–55. Panels A and C show a between/within decomposition of the variance of earnings changes within the formal-formal (panel A) and informal-informal (panel C) worker groups based on equation (4) across four education groups. Panels B and D show shift-share analyses of the within-education group component of equation (4) across four education groups within the formal-formal (panel B) and informal-informal (panel D) worker groups. Returns channel means holding the education composition fixed at its initial level and letting the within-group variances evolve as in the data. Composition channel means holding the within-group variances fixed at their initial level and letting the education composition evolve as in the data. *Source*: PME, 2002–2015.

2012

Composition channel

2006

2010

2014

2004

group component in the same spirit as above. We focus on educational composition because Brazil experienced a rapid increase in educational attainment over this period.¹

Figure E.1 plots the results of these exercises. As noted above, the great majority of the decline in the volatility of earnings among formal-formal and informal-informal workers is accounted for by the within component. The great majority of the fall in the within component is, in turn, driven by changes within education groups in the variance of earnings, as opposed to changes in the educational composition of the workforce combined with differences across education groups in their volatility of earnings.

¹In unreported results, we find that compositional shifts in other demographic dimensions such as age and gender account for relatively little of the overall decline in the variance of residual log earnings changes over this period.

The reason is that although Brazil has seen rapid changes in educational composition over this period, the differences across education groups in the within-education group volatility of earnings are not that large. While the findings of this type of accounting exercise in the absence of an equilibrium model should be cautiously interpreted, at face value, they do suggest a limited role for rising educational attainment in driving the fall in earnings volatility among formal-formal and informal-informal workers.

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Co-editor Giovanni L. Violante handled this manuscript.

Manuscript received 24 February, 2021; final version accepted 18 February, 2022; available online 23 March, 2022.