# Supplement to "Earnings inequality and dynamics in the presence of informality: The case of Brazil" 

(Quantitative Economics, Vol. 13, No. 4, November 2022, 1405-1446)

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We provide additional summary statistics in Appendix A. We present additional figures for Brazil's formal sector in Appendix B. We present additional figures for Brazil's informal sector in Appendix C. We discuss the role of multiple job holdings in Appendix D. We demonstrate the limited role of demographics in explaining the decline of the variance of residual log earnings changes in Appendix E.

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## Appendix A: Additional summary statistics

Table A.1. Cross-sectional summary statistics, overall.
$\begin{array}{lllllllllllll}\text { Year Obs. Mean Std. dev. P1 } & \text { P5 } & \text { P10 } & \text { P25 } & \text { P50 } & \text { P75 } & \text { P90 } & \text { P95 } & \text { P99 } & \text { P99.9 } & \text { P99.99 }\end{array}$

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1985 15.7 19,852 26,915 585 1755 3121 5881 11,105 22,696 44,737 67,256 134,110 255,402 425,948
1986 16.9 20,627 26,716 635 1751 3038 5932 11,865 24,215 47,043 69,680 134,984 224,955 387,154
1987 17.6 18,824 27,220 429 1364 2496 5009 10,438 21,323 42,172 64,080 134,699 290,922 403,407
1988 18.6 18,859 27,307 291 1148 2430 4910 10,045 21,266 42,977 66,632 137,842 256,362 396,512
1989 19.3 18,591 27,174 231 935 2319 4835 9839 20,902 41,922 65,923 139,556 254,659 387,672
1990 19.7 15,268 21,970 232 962 1873 3766 8078 17,521 34,687 54,200 112,631 199,526 297,985
1991 19.5 14,533 20,786 319 1021 1915 3861 7833 16,536 32,834 51,001 104,857 192,177 315,036
1992 19.4 14,399 20,297 202 826 1804 3936 7844 16,229 33,058 50,913 101,826 189,134 277,698
1993 20.1 15,728 23,111 162 766 1899 4178 8239 17,393 36,211 56,422 117,313 217,039 324,278
1994 20.7 16,524 23,245 244 1046 2074 4260 8671 18,903 38,908 58,775 117,161 211,849 305,908
1995 21.8 19,214 27,671 502 1345 2336 4723 9921 21,786 45,038 69,210 141,114 253,044 348,350
1996 21.9 19,335 27,785 574 1457 2468 4991 10,250 21,771 44,745 68,389 141,832 262,035 373,896
1997 22.3 19,434 28,048 594 1518 2552 5099 10,342 21,726 44,565 68,732 143,569 264,084 384,921
1998 22.9 19,869 29,077 623 1581 2687 5301 10,594 22,129 44,593 69,648 148,988 282,161 412,739
1999 23.1 19,153 28,001 613 1544 2628 5230 10,257 21,224 42,486 67,007 144,740 271,705 392,265
2000 23.7 19,013 28,187 608 1516 2613 5214 10,116 20,932 42,019 66,764 146,056 276,394 393,854
2001 25.4 19,133 29,659 619 1543 2648 5268 9954 20,582 42,124 66,775 151,038 311,010 464,091
2002 26.4 18,756 30,505 623 1551 2660 5292 9708 20,055 41,195 65,011 147,759 313,361 474,376
2003 27.4 17,699 27,930 596 1527 2596 5170 9236 18,791 38,405 60,946 138,945 306,786 475,542
2004 28.8 18,017 28,201 623 1600 2730 5386 9543 19,086 39,022 61,793 140,291 305,658 486,266
2005 30.5 17,974 28,196 628 1614 2752 5533 9554 18,908 38,617 61,227 140,834 304,485 489,218
2006 32.3 18,645 29,425 664 1736 2955 5992 9892 19,412 39,774 62,802 145,559 335,661 522,767
2007 34.2 18,996 29,772 681 1781 3055 6261 10,154 19,745 40,513 63,629 147,545 339,696 530,402
2008 36.5 19,464 30,495 722 1884 3173 6445 10,413 20,210 41,296 64,882 151,420 339,068 544,611
2009 37.9 19,866 30,908 721 1864 3209 6813 10,740 20,559 42,126 66,313 154,799 333,382 551,067
2010 40.4 20,392 31,395 773 2017 3451 7150 11,161 21,166 42,969 67,674 156,655 339,306 568,684
2011 42.4 20,773 31,431 804 2081 3547 7277 11,545 21,745 43,702 68,351 156,676 333,256 582,293
2012 43.9 21,589 31,614 858 2247 3841 7886 12,290 22,813 45,472 70,051 157,155 326,983 577,155
2013 45.1 22,085 31,783 887 2326 3942 8120 12,692 23,572 46,434 71,300 158,852 328,978 587,556
2014 45.9 22,602 32,090 924 2454 4104 8313 13,143 24,181 47,504 72,443 161,116 331,021 589,361
2015 44.9 22,566 31,988 929 2509 4242 8457 13,199 23,947 47,263 72,238 160,124 336,925 588,808
2016 43.0 22,342 30,764 954 2577 4363 8665 13,312 23,864 46,388 70,941 154,707 317,613 563,472
2017 42.3 22,882 31,395 975 2660 4498 8940 13,702 24,396 47,287 72,435 158,572 317,728 571,961
201842.5 22,641 30,825 985 2687 4534 8889 13,566 24,124 46,854 71,716 155,823 310,005 562,571
```

Note: Workers aged 25-55. Source: RAIS, 1985-2018.

Table A.2. Cross-sectional summary statistics, men only.

|  |  |  |  |  |  |  |  |  |  |  |  | P99.9 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 29, |  | 1810 |  |  |  |  |  |  |  |  |  |
|  | , | 29, | 694 | 1908 | 33 | 6467 | 12,983 |  |  |  |  |  |  |
|  | 20,6 | 29,192 | 478 | 1483 | 27 | 66 | 11,583 |  |  |  |  |  |  |
|  | 12.5 20,678 | 29,802 | 310 | 1199 | 252 | 5287 | 11,099 | 23 |  | 73,964 |  |  |  |
|  | 12.9 20,447 | 29, | 42 | 954 | 239 | 5206 | 10,947 | 22 | 46,691 | 73,473 | 52 | 269 |  |
| 1990 | 13.0 16,529 | 23,716 | 246 | 1002 | 195 | 39 | 8869 | 18 |  | 9,386 |  | 10,5 |  |
|  | 15,800 | 22 | 335 | 1052 |  | 9 | 8597 |  |  |  |  |  |  |
|  | 15 | 22,315 | 208 | 21 |  |  | 8613 |  |  |  |  |  |  |
|  | $13.117,225$ | 25 | 166 | 747 |  | 4356 | 9037 |  |  |  |  |  |  |
|  | $13.417,821$ | 25,239 | 248 | 1050 | 20 | 70 | 939 |  |  |  |  |  |  |
|  | 20 | 29, | 524 | 1399 | 24 | 45 | 10,859 | 23 | 3 | 75 | 53,967 | 265,98 | 369,637 |
| 1996 | 20 | 30, | 599 | 15 | 25 | 5301 | 11, | 23 |  | 75,210 | 154,839 | 276,879 |  |
|  | 20, | 30,399 | 612 | 1533 | 261 | 5362 | 11,132 |  |  |  |  |  |  |
|  | 21, | 31,347 | 638 | 159 |  | 5548 | 11,307 |  |  |  |  |  |  |
|  | 20 | 30,187 | 628 | 1539 |  | 0 | 10,891 |  |  |  |  |  |  |
|  | 19 | 30,046 | 28 | 152 |  | 5381 | 10,710 |  |  |  |  |  |  |
|  | 20 | 32,017 | 629 | 155 | 26 | 68 | 10 |  |  |  |  |  |  |
|  | 16.2 19, | 33, |  | 15 |  | 5469 | 10, |  |  |  |  |  |  |
|  | 18, | 30, | 628 | 15 | 26 |  | 987 |  |  |  |  |  |  |
|  | 19,0 | 30,457 | 663 | 162 | 27 | 5575 | 10,110 |  |  |  |  | 331 |  |
|  | 19 | 30,436 | 668 | 167 |  | 5721 | 10,205 |  |  |  |  |  |  |
|  | 19 | 31, | 712 | 18 |  |  | 10 |  |  |  |  |  |  |
|  | 20,062 | 31,930 | 740 | 18 |  |  | 10,916 |  |  |  |  |  |  |
|  | $21.820,638$ | 32,709 | 804 | 2031 | 33 | 95 | 11,283 |  |  |  | 65,123 | 359,067 |  |
|  | 22.421, | 33,154 | 785 | 2000 | 33 | 388 | 11,570 |  |  |  | 68 | 55 |  |
|  | 23.7 21,6 | 33,744 | 867 | 2218 | 36 | 62 | 12, |  |  |  |  |  |  |
|  | 22,178 | 33,898 | 02 | 2317 | 3825 | 7579 | 12,608 |  |  |  |  |  |  |
|  | 23 | 34,277 | 97 | 2503 |  | 8219 | 13 | 24 | 47,239 |  |  |  |  |
|  | 23,691 | 34,468 | 999 | 2582 |  | 35 | 14, |  |  |  |  | 359 |  |
|  | 26.0 24,235 | 34,812 | 1042 | 2652 | 44 | 8709 | 14,489 |  |  |  | 76,476 | 362 |  |
|  | 25.3 24,077 | 34,642 | 1014 | 2641 |  | 8773 | 14,463 | 25,2 | 49,16 | 76,8 | 5,2 | 64 |  |
|  | $24.123,693$ | 33,301 | 1021 | 2679 | 44 | 8929 | 14,448 | 25,0 | 48,13 | 75,243 | 168,9 |  |  |
|  | 23.6 24,233 | 33,968 | 1037 | 2743 | 459 | 9190 | 14,788 | 25,50 | 49,042 | 76,94 | , | 46,9 | 9 |
| 018 | 23.7 23,919 | 33,340 | 1053 | 2763 | 4650 | 190 | 14,606 | 25,13 | 8,41 | 5, | 68,979 | 40,03 | 5,497 |

Note: Workers aged 25-55. Source: RAIS, 1985-2018.

Table A.3. Cross-sectional summary statistics, women only.

|  | Obs. |  |  |  |  |  |  |  |  |  |  |  | P99.9 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | 546 |  |  | 5203 |  |  |  |  | 0 | 170,577 |  |
|  |  | 14,943 | 22 | 35 | 42 | 21 | 20 | 41 |  |  | 48,978 | 95,853 |  | 390,751 |
|  |  | 15 | 20,772 |  | 1049 | 22 | 4415 | 30 | 17,418 | 34,025 | 51,686 | 107,098 | 189,608 | 326,275 |
|  |  | 14 | 20,777 |  | 996 | 220 |  | 827 | 17,087 |  | 49,989 | 106,495 |  |  |
|  |  | 12,811 | 17,837 | 208 |  |  |  |  |  |  |  | 90,607 |  |  |
|  |  |  |  | 295 |  |  |  | 540 | 14,030 |  |  | 2,045 | 155,255 |  |
|  |  | 11, |  | 193 |  | 82 | 08 | 61 |  | 26, | 39,789 | 75,928 | 143 |  |
|  | 7.0 | 12,953 | 18 | 157 | 79 | 197 | 84 | 702 | 14 | 28,827 | 44,341 | 92,373 | 170,239 | 253,249 |
|  |  | 14 | 18,880 | 240 | 1042 | 2036 | 3981 | 49 |  |  |  | 93,499 | 168,105 |  |
|  |  | 16,297 | 22,808 |  |  |  |  | 8455 |  |  |  |  |  |  |
|  |  |  |  |  | 1378 |  |  | 8977 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  | 9182 |  |  |  |  | 222,966 |  |
|  | 8.5 | 17 | 24 | 596 | 1557 | 26 | 5012 | 9538 | 20 | 40,835 |  | 123,556 | 238,938 | 355,660 |
|  |  | 17 | 23 | 5 | 1545 | 26 | 03 | 934 | 19 | 39,492 | 58,859 | 120,402 | 232,289 | 338,864 |
|  |  |  |  | 58 |  |  |  | 922 |  |  |  |  |  |  |
|  | 9.7 | 17 | 25,295 | 579 | 1506 |  |  | 901 |  |  |  |  |  |  |
|  | 10.2 | 17,137 | 25, |  | 1520 |  | 5069 | 889 |  |  |  |  |  | 12,300 |
|  | 10 | 16 | 23 | 56 |  |  | 5029 |  |  |  |  |  |  |  |
|  |  |  | 2 | 582 |  |  |  | 8645 |  |  |  |  |  |  |
|  | 12 | 16 | 24 | 58 |  |  |  | 860 |  | 36,366 |  |  |  |  |
|  | 12 | 17, | 25 |  |  | 285 | 5822 | 893 |  |  |  |  | 289,308 |  |
|  | 13 | 17, | 26, | 62 |  | 28 |  | 9150 | 18, |  |  |  |  |  |
|  | 14.8 |  | 26 |  |  |  |  | 932 |  |  |  |  | 302,464 |  |
|  | 15 | 18, |  |  |  | 298 | 19 | 9675 |  |  |  |  |  |  |
|  |  | 18 |  | 690 |  |  | 5 | 99 |  |  |  |  |  |  |
|  | 17.7 | 18,8 | 27, | 71 | 1856 | 31 | 76 | 10,2 |  |  | 62,755 | 135,569 | 298 |  |
|  | 18.6 | 19,580 | 27, | 76 | 2010 | 345 | 75 | 10,90 |  |  | 64,598 | 136,492 | 90 |  |
|  | 19.3 | 19,9 |  | 788 | 208 | 358 | 7824 | 11,27 |  |  |  |  | 90 |  |
|  | 19.8 | 20,460 | 27,979 | 82 | 2190 |  | 799 | 11,718 |  |  | 66,901 | , | , | , |
|  | 19.6 | 20,616 | 28,076 | 84 | 2318 | 400 | 41 | 11,855 | 21, | ,813 | 66,863 | 139, | 298, |  |
|  | 18.9 | 20,621 | 27,094 | 88 | 455 | 422 | 442 | 12,094 | 22,078 | 4,39 | 65,828 | 135,63 | 281, |  |
| 2017 | 18.7 | 21,179 | 27,723 | 91 | 41 | 438 | 72 | 12,532 | 22,613 | 45,282 | 67,255 | 139,690 | 280,049 | 59,173 |
| 018 | 18.9 | 21,038 | 27,260 | 923 | 2544 | 4376 | 8684 | 12,472 | 22,49 | 45,130 | 66,793 | 137,60 | 274,721 | 47,1 |

Note: Workers aged 25-55. Source: RAIS, 1985-2018.

Appendix B: Additional figures for Brazil's formal sector


Figure B.1. Evolution of earnings percentiles, men and women pooled. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.2. Evolution of earnings percentiles, men and women pooled and controlling for age.
Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.3. Evolution of residual earnings percentiles, men and women pooled and controlling for age and education. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.4. Pareto tail within top $1 \%$, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.
(a) Men

(b) Women


Figure B.5. Pareto tail within top 5\%, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.
(a) Income shares of quintiles

(b) Selected income shares


Figure B.6. Evolution of earnings shares, relative to 1995. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.7. Gini coefficient of earnings. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.8. Dispersion in 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.9. Higher-order moments of the distribution of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.
(a) P90-P10, men
(b) P90-P10, women

(c) Kelley skewness, men

(e) Excess Crow-Siddiqui kurtosis, men


(d) Kelley skewness, women

(f) Excess Crow-Siddiqui kurtosis, women


Figure B.10. Moments of the distribution of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1999-2018.


Figure B.11. Standardized moments of the distribution of 1-year earnings changes, by gender. Note: Workers aged 25-55. Skewness corresponds to the standardized third moment of the distribution. Excess kurtosis is defined as the standardized fourth moment of the distribution minus 3. Source: RAIS, 1999-2018.
(a) P90-P10, men

(c) Kelley skewness, men

(e) Excess Crow-Siddiqui kurtosis, men

(b) P90-P10, women

(d) Kelley skewness, women

(f) Excess Crow-Siddiqui kurtosis, women


Figure B.12. Moments of the distribution of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1999-2018.


Figure B.13. Standardized moments of the distribution of 5 -year earnings changes, by gender. Note: Workers aged 25-55. Skewness corresponds to the standardized third moment of the distribution. Excess kurtosis is defined as the standardized fourth moment of the distribution minus 3. Source: RAIS, 1999-2018.
(a) Men

(b) Women


Figure B.14. Evolution of earnings mobility over the life cycle, by gender. Note: Workers aged 25-55. Colored markers denote the top $0.1 \%$ of permanent income $P_{i t}$. Source: RAIS, 1985-2018.


Figure B.15. Evolution of earnings mobility over time, by gender. Note: Workers aged 25-55. Colored markers denote the top 0.1\% of permanent income $P_{i t}$. Source: RAIS, 1985-2018.


Figure B.16. Density of 1-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.
(a) Men
(b) Women



Figure B.17. Density of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.
(a) Men
(b) Women



Figure B.18. Log density of 1-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.


Figure B.19. Log density of 5-year earnings changes, by gender. Note: Workers aged 25-55. Source: RAIS, 1985-2018.

Appendix C: Additional figures for Brazil's informal sector

## (a) Formal-formal transitions <br> (b) Informal-informal transitions




Figure C.1. Education shares, by origin and destination sector. Note: Workers aged 25-55. Source: PME, 2002-2015.


Figure C.2. Age group shares, by origin and destination sector. Note: Workers aged 25-55. Source: PME, 2002-2015.


Figure C.3. Densities of log earnings, by sector and population subgroup in 2002. Note: Workers aged $25-55$. Kernel densities of log earnings by worker group. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. Source: PME, 2002.


Figure C.4. Densities of log earnings, by sector and population subgroup in 2015. Note: Workers aged 25-55. Kernel densities of log earnings by worker group. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. Source: PME, 2015.


Figure C.5. Densities of residual log earnings, by sector and population subgroup in 2002. Note: Workers aged 25-55. Kernel densities of residual log earnings by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. Source: PME, 2002.


Figure C.6. Densities of residual log earnings, by sector and population subgroup in 2015. Note: Workers aged 25-55. Kernel densities of residual log earnings by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines show the overall distribution as well as that in the formal sector and that in the informal sector. Source: PME, 2015.
(a) Men, <HS, age 25-34
(b) Men, <HS, age 35-44
(c) Men, <HS, age 45-55

(d) Men, $\geq$ HS, age 25-34

(g) Women, <HS, age 25-34

(j) Women, $\geq$ HS, age 25-34


(e) Men, $\geq$ HS, age 35-44

(h) Women, <HS, age 35-44

(k) Women, $\geq$ HS, age 35-44


(f) Men, $\geq$ HS, age $45-55$

(i) Women, < HS, age 45-55

(l) Women, $\geq$ HS, age $45-55$


Figure C.7. Densities of 1-year residual log earnings changes, by transition type and population subgroup in 2002-2003. Note: This figure shows kernel densities of 1-year changes in residual log earnings for workers aged 25-55 by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines denote different combinations of a worker's current sector of employment and that in the next survey wave (e.g., "Formal-Informal" denotes current employment in the formal sector and employment in the informal sector in the next survey wave). Source: PME, 2002-2003.
(a) Men, <HS, age 25-34
(b) Men, <HS, age 35-44
(c) Men, <HS, age 45-55

(d) Men, $\geq$ HS, age 25-34

(g) Women, <HS, age 25-34

(j) Women, $\geq$ HS, age 25-34


(e) Men, $\geq$ HS, age 35-44

(h) Women, <HS, age 35-44

(k) Women, $\geq$ HS, age 35-44


(f) Men, $\geq$ HS, age $45-55$

(i) Women, < HS, age 45-55

(l) Women, $\geq$ HS, age $45-55$


Figure C.8. Densities of 1-year residual log earnings changes, by transition type and population subgroup in 2014-2015. Note: This figure shows kernel densities of 1-year changes in residual log earnings for workers aged 25-55 by worker group. Residuals are calculated controlling for age and survey wave fixed effects, separately by gender and year. Different lines denote different combinations of a worker's current sector of employment and that in the next survey wave (e.g., "Formal-Informal" denotes current employment in the formal sector and employment in the informal sector in the next survey wave). Source: PME, 2014-2015.

Table D.1. Evolution of multiple-job-holding rates.

|  | Panel A. Formal sector |  |  |  | Panel B. Informal sector |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2002-04 | 2005-08 | 2009-11 | 2012-15 | 2002-04 | 2005-08 | 2009-11 | 2012-15 |
| Share with secondary job (\%) | 2.8 | 2.9 | 2.7 | 2.3 | 2.1 | 2.3 | 2.1 | 2.2 |
| Mean weekly hours in main job | 42.8 | 42.5 | 42.3 | 42.0 | 41.8 | 41.6 | 41.0 | 40.3 |
| Mean weekly hours in secondary jobs | 17.5 | 17.2 | 15.0 | 16.7 | 22.2 | 21.8 | 20.2 | 21.6 |
| Share with SS contributions in secondary job | 51.2 | 52.2 | 54.4 | 59.1 | 25.0 | 23.5 | 25.7 | 30.9 |

Note: Workers aged 25-55. Share of formal or informal employment with a secondary job. "Mean weekly hours in main job" is for the full sample population conditional on holding a job. "Mean weekly hours in secondary jobs" includes hours worked in all nonprimary (i.e., secondary, tertiary, etc.) jobs and is computed among the subpopulation of workers with more than one concurrent job. Source: PME, 2002-2015.

## Appendix D: The role of multiple job holdings

One may wonder whether the decrease in the informal employment share in Brazil is driven by changes in the prevalence of workers concurrently holding multiple jobs with a mix between formal and informal employment. To investigate this, Table D. 1 summarizes the share of workers who hold multiple jobs in a month, broken down by whether the main job is in the formal sector (panel A) or informal sector (panel B). Holding multiple job is not particularly common in Brazil, with roughly $2 \%$ of employed workers holding multiple jobs. The fraction is modestly lower among informal sector workers. Among formal sector workers with a second job, roughly half of them contribute to social security in their second job (a proxy for the formality status of the second job). Moreover, the (un)importance of holding multiple jobs has remained roughly stable over time. Hence, the main margin of formalization is the extensive margin-workers switching entirely into the formal sector-as opposed to a declining prevalence of workers holding multiple jobs in both the informal and formal sector.

## Appendix E: The limited role of demographics in explaining the decline in the variance of residual log earnings changes

We here present a between- versus within-group decomposition similar to that in equation (4) of Section 4.1.4 of the main text (Engbom, Gonzaga, Moser, and Olivieri (2022)). Specifically, we decompose the overall variance of earnings changes for workers undergoing formal-formal and informal-informal sector transitions into between and within components by worker subgroups. Specifically, we focus on worker subgroups by four education groups. We restrict attention to the formal-formal and informal-informal worker groups because they constitute the great majority of Brazilian employment. Motivated by the fact that the within-education group component accounts for the great majority of changes in the volatility of earnings among formal-formal and informalinformal workers, we further consider a shift-share analysis of the within-education
(a) Between vs. within, formal-formal

(c) Between vs. within, informal-informal



Figure E.1. The role of changes in educational attainment. Note: Workers aged 25-55. Panels A and C show a between/within decomposition of the variance of earnings changes within the formal-formal (panel A) and informal-informal (panel C) worker groups based on equation (4) across four education groups. Panels B and D show shift-share analyses of the within-education group component of equation (4) across four education groups within the formal-formal (panel B) and informal-informal (panel D) worker groups. Returns channel means holding the education composition fixed at its initial level and letting the within-group variances evolve as in the data. Composition channel means holding the within-group variances fixed at their initial level and letting the education composition evolve as in the data. Source: PME, 2002-2015.
group component in the same spirit as above. We focus on educational composition because Brazil experienced a rapid increase in educational attainment over this period. ${ }^{1}$

Figure E. 1 plots the results of these exercises. As noted above, the great majority of the decline in the volatility of earnings among formal-formal and informal-informal workers is accounted for by the within component. The great majority of the fall in the within component is, in turn, driven by changes within education groups in the variance of earnings, as opposed to changes in the educational composition of the workforce combined with differences across education groups in their volatility of earnings.

[^1]The reason is that although Brazil has seen rapid changes in educational composition over this period, the differences across education groups in the within-education group volatility of earnings are not that large. While the findings of this type of accounting exercise in the absence of an equilibrium model should be cautiously interpreted, at face value, they do suggest a limited role for rising educational attainment in driving the fall in earnings volatility among formal-formal and informal-informal workers.

## References

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Co-editor Giovanni L. Violante handled this manuscript.
Manuscript received 24 February, 2021; final version accepted 18 February, 2022; available online 23 March, 2022.


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[^1]:    ${ }^{1}$ In unreported results, we find that compositional shifts in other demographic dimensions such as age and gender account for relatively little of the overall decline in the variance of residual log earnings changes over this period.

