# Supplement to "Experimenting with the transition rule in dynamic games" 

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This file provides a number of supplementary analyses and tables to the main paper.

Table S.I. Unique MPE in an endogenous game.

| Player $i / j$ | $M_{D D}$ | $M_{C D}$ | $M_{D C}$ | $M_{C C}$ |
| :--- | :---: | :--- | :--- | :--- |
| $M_{D D}$ | SPE | Player $j$ deviates to $D$ in low | Player $j$ deviates to $D$ in <br> high | Player $j$ deviates to $D$ in low |
| $M_{C D}$ | - | Either player deviates to $D$ | Player $i$ deviates to $D$ in low <br> in low | Player $j$ deviates to $D$ in low <br> in high player deviates to $D$ |
| $M_{D C}$ | - |  |  | Either player deviates to $D$ <br> in high |
| $M_{C C}$ | - | - | Either player deviates to $D$ <br> in high |  |

[^0]Table S.II. Initial cooperation rates.

| State | Easy |  |  | Difficult |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Static | Exog. | Endog. | Static | Exog. | Endog. |
| Initial cooperation (all supergames) |  |  |  |  |  |  |
| Low | 0.726 | 0.719 | 0.822 | 0.602 | 0.591 | 0.841 |
|  | (0.049) | (0.057) | (0.053) | (0.061) | (0.061) | (0.042) |
| High | 0.676 | 0.552 | 0.834 | 0.356 | 0.316 | 0.678 |
|  | (0.060) | (0.053) | (0.54) | (0.055) | (0.053) | (0.062) |
| Initial cooperation (last five supergames) |  |  |  |  |  |  |
| Low | 0.736 | 0.733 | 0.824 | 0.558 | 0.610 | 0.886 |
|  | (0.062) | (0.063) | (0.057) | (0.076) | (0.069) | (0.047) |
| High | 0.692 | 0.510 | 0.800 | 0.300 | 0.302 | 0.653 |
|  | (0.067) | (0.070) | (0.066) | (0.064) | (0.063) | (0.065) |

Note: The initial cooperation rate captures the frequency of $C$ choices in each state using the first choice a subjects make in that state within the supergame. In the case of the low state, only period-one choices are included.

Table S.III. Aggregate cooperation (last five supergames).

|  | Unweighted |  |  |  | State-Matched |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Param. |  |  |  | Param. |  |
| Transition | Easy | Diff. |  | $\Delta_{\Psi}$ |  | Easy |
| Static | 0.604 | 0.351 | -0.252 |  | 0.595 | 0.319 |
|  | $(0.049)$ | $(0.044)$ | $(0.065)$ |  | $(0.050)$ | $(0.042)$ |
| Exogenous | 0.561 | 0.383 | -0.177 |  | 0.548 | 0.357 |
|  | $(0.049)$ | $(0.047)$ | $(0.067)$ |  | $(0.050)$ | $(0.047)$ |
| Endogenous | 0.633 | 0.613 | -0.020 | 0.633 | 0.613 |  |
|  | $(0.046)$ | $(0.035)$ | $(0.058)$ | $(0.046)$ | $(0.035)$ |  |

Note: Coefficients in the first two data columns (and standard errors accounting for 252 subject clusters) are recovered from a linear probability model with six treatment-dummy regressors. Coefficients in the state-weighted column are derived from a similar model with the following set of mutually exclusive dummy variables: (i) a treatment dummies for the two Endogenous treatments, with coefficients representing $\hat{\operatorname{Pr}\left\{C \mid \Psi_{X}\right\} \text {; and (ii) treatment-state-period dummies for the exogenous treatments, }}$ with coefficients representing $\hat{\operatorname{Pr}\left\{C \mid t, \theta, \Psi_{X}\right\} \text {. Reported coefficients for the Exogenous and Static treatments reflect the weighted }}$ sum $Q\left(\Psi_{X}\right)$ across the relevant treatment-state-period coefficient to correct for differing state selection.

Table S.IV. P-values of hypothesis tests between initial cooperation rates (last five supergames).

|  | $S_{L}^{\text {Esy }}$ | $S_{L}^{\text {Dif }}$ | $S_{H}^{\text {Esy }}$ | $S_{H}^{\text {Dif }}$ | $E x_{L}^{\text {Esy }}$ | $E x_{L}^{\text {Dif }}$ | $E x_{H}^{\text {Esy }}$ | $E x_{H}^{\text {Dif }}$ | $E n_{L}^{\text {Esy }}$ | $E n_{L}^{\text {Dif }}$ | $E n_{H}^{\text {Esy }}$ | $E n_{H}^{\text {Dif }}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $S_{L}^{\text {Esy }}$ | - | 0.072 | 0.528 | 0.000 | 0.977 | 0.176 | 0.017 | 0.000 | 0.301 | 0.056 | 0.480 | 0.358 |
| $S_{L}^{\text {Dif }}$ | - | - | 0.187 | 0.001 | 0.078 | 0.619 | 0.642 | 0.010 | 0.006 | 0.000 | 0.017 | 0.345 |
| $S_{H}^{\text {Esy }}$ | - | - | - | 0.000 | 0.656 | 0.391 | 0.061 | 0.000 | 0.137 | 0.019 | 0.253 | 0.673 |
| $S_{H}^{\text {Dif }}$ | - | - | - | - | 0.000 | 0.001 | 0.028 | 0.983 | 0.000 | 0.000 | 0.000 | 0.000 |
| $E x_{L}^{E s y}$ | - | - | - | - | - | 0.187 | 0.000 | 0.000 | 0.289 | 0.053 | 0.465 | 0.375 |
| $E x_{L}^{\text {Dif }}$ | - | - | - | - | - | - | 0.313 | 0.000 | 0.018 | 0.001 | 0.047 | 0.648 |
| $E x_{H}^{\text {Esy }}$ | - | - | - | - | - | - | - | 0.028 | 0.001 | 0.000 | 0.003 | 0.136 |
| $E x_{H}^{D i f}$ | - | - | - | - | - | - | - | - | 0.000 | 0.000 | 0.000 | 0.000 |
| $E n_{L}^{\text {Esy }}$ | - | - | - | - | - | - | - | - | - | 0.405 | 0.784 | 0.050 |
| $E n_{L}^{D i f}$ | - | - | - | - | - | - | - | - | - | - | 0.290 | 0.004 |
| $E n_{H}^{\text {Esy }}$ | - | - | - | - | - | - | - | - | - | - | - | 0.113 |
| $E n_{H}^{D i f}$ | - | - | - | - | - | - | - | - | - | - | - | - |


#### Abstract

Note: To compute these $p$-values, we first run a regression in which the unit of observation is the choice a subject makes in a period of a supergame. The sample is constrained to the last five supergames and to periods in which the subject makes the first choice in each state. The dependent variable takes value 1 if the subject decided to cooperate and 0 otherwise. The right-hand side includes a fully saturated set of dummies that account for differences in cooperation rates across three dimensions: the treatment (Easy-Endog, Easy-Exog, Easy-Static, Easy-Endog, Easy-Exog, Easy-Static), the state (Low, High). Standard errors are clustered by subject. The table reports the $p$-values of bilateral comparisons between coefficients for the treatment cross state dummies. The table reports the $p$-value of a $t$-test in which the null hypothesis is Row Estimate = Column Estimate. There is one row per (initial-cooperation rate) coefficient estimate and one column per (initial-cooperation rate) coefficient, where notation is as follows. $S, E x$, and En capture whether the coefficient corresponds to a static, exogenous, or endogenous treatment, respectively. The superscript (Esy, Dif) identifies if the coefficient corresponds to a easy or difficult parameterization, respectively. The subscript ( $L, H$ ) identifies if the coefficient corresponds to behavior in the low or high state, respectively. 


Table S.V. Common sequences of actions as percent of histories (last five supergames).

| Treatment |  | Five or more observed supergames |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Easy-Endog | CC, CC, CC, CC, CC | DC, DD, DD, DD, DD | CC, DC, DC, DD, DC | DC, DC, DD, DD, DD |
|  | 37.1 | 10.5 | 6.7 | 4.8 |
| Diff-Endog | CC, CC, CC, CC, CC | CC, DC, DD, DC, DD | CC, CC, CC, CC, DC | CC, DC, DD, DD, DD |
|  | 20.0 | 6.7 | 5.7 | 4.8 |
| Easy-Exog | CC, CC, CC, CC, CC | DC, DD, DD, DD, DD | DD, DD, DD, DD, DD |  |
|  | 36.2 | 20.0 | 5.7 |  |
| Diff-Exog | DC, DD, DD, DD, DD | DD, DD, DD, DD, DD | CC, CC, CC, CC, CC | DC, DC, DD, DD, DD |
|  | 22.9 | 18.1 | 18.1 | 4.8 |
| Easy-Static (low) | CC, CC, CC, CC, CC | DC, DD, DD, DD, DD | DC, DC, DD, DD, DD |  |
|  | 50.9 | 18.9 | 9.4 |  |
| Diff-Static (low) | CC, CC, CC, CC, CC | DC, DD, DD, DD, DD | DD, DD, DD, DD, DD | DC, DC, DD, DD, DD |
|  | 25.0 | 20.0 | 13.3 | 11.7 |
| Easy-Static (high) | CC, CC, CC, CC, CC | DC, DD, DD, DD, DD | DD, DD, DD, DD, DD |  |
| Diff-Static (high) | DD, DD, DD, DD, DD | DC, DD, DD, DD, DD | 9.6 |  |
|  | 46.7 | 22.2 |  |  |

Note: In endogenous and static-transition treatments, high-state action pairs are displayed in bold face.

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