

ONLINE APPENDIX to
“Income Risk Inequality: Evidence from Spanish
Administrative Records”

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Abstract

This appendix provides additional results that complement the paper and the main appendix. In Online Appendix [S-A](#), we report additional results relating to Section [3](#) of the paper. In Online Appendix [S-B](#) we detail the calculations of the welfare cost of risk. In Online Appendix [S-C](#) we report the coefficients in the Poisson regressions used in the CV measure in Sections [4](#) and [5](#) in the paper. In Online Appendix [S-D](#) we show how we account for unobserved heterogeneity. In Online Appendix [S-E](#) we provide details about quantile estimation. In Online Appendix [S-F](#) we describe how we estimate subjective income expectations. Lastly, in Online Appendix [S-G](#) we report additional results regarding the robustness checks performed in the paper.

S-A Additional tables and figures on income inequality and dynamics

Table S-A1: Descriptive statistics for the CS sample

(a) Panel A: Basic summary statistics

Year	Obs ($\times 1000$)	Mean Income		Females	Age Shares %			Education Shares %			
		Males	Females	% Share	[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2005	415	30064	21363	43.8	44.6	33.3	22.1	14.5	36.5	28.2	20.7
2006	435	30532	21863	44.3	43.6	33.7	22.7	14.3	36.6	27.8	21.3
2007	455	30905	22400	44.8	42.8	34.1	23.1	14.1	36.7	27.5	21.6
2008	463	30786	22788	45.6	41.6	34.6	23.8	13.7	36.6	27.4	22.3
2009	444	30676	23347	46.3	39.7	35.4	25.0	12.7	36.3	27.6	23.5
2010	433	30094	22916	46.8	38.0	36.1	25.9	12.1	36.4	27.5	24.1
2011	425	29280	22132	47.3	36.4	36.9	26.8	11.6	36.4	27.4	24.6
2012	407	28140	21387	47.6	34.5	37.8	27.7	11.1	35.8	27.6	25.6
2013	396	27294	21141	47.5	32.7	38.6	28.7	11.1	35.8	27.2	25.9
2014	397	27087	21209	47.3	31.4	39.0	29.5	11.2	35.9	26.8	26.1
2015	405	27605	21650	47.4	30.3	39.2	30.5	11.2	35.9	26.5	26.4
2016	409	28119	22153	47.4	29.5	39.1	31.4	11.1	35.7	26.3	26.8
2017	415	28153	22174	47.5	29.0	38.7	32.3	11.1	35.6	26.1	27.2
2018	420	28504	22479	47.6	28.7	37.9	33.4	11.0	35.4	26.1	27.6

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2005	1866	4166	6972	13860	21235	31997	47977	62769	106369	133741
2006	1940	4455	7426	14360	21596	32453	48514	63223	106207	133169
2007	1990	4562	7616	14580	21867	32889	49210	63959	108446	136093
2008	1969	4357	7184	14101	21981	33179	49809	64652	109276	136193
2009	1887	3786	6285	13411	22150	33876	51115	65667	111121	137111
2010	1869	3695	6082	13044	21788	33330	50055	64478	109173	134855
2011	1827	3568	5864	12488	21217	32283	48434	62656	105661	131472
2012	1719	3260	5396	11837	20509	31093	46591	60896	101702	127134
2013	1661	2988	4864	10976	19965	30737	46361	60020	99412	125199
2014	1684	3039	4929	10897	19847	30712	46202	59883	100242	126201
2015	1736	3253	5306	11337	20031	31056	47057	60888	103314	130508
2016	1804	3567	5811	12043	20448	31465	47567	61494	104497	132484
2017	1962	3855	6239	12520	20465	31277	47052	60913	103168	130550
2018	2026	4119	6691	13050	20802	31492	46947	60816	103516	130403

Notes: CS sample. Annual earnings are reported in 2018 U.S. dollars.

Table S-A2: Descriptive statistics for the LS sample

(a) Panel A: Basic summary statistics

Year	Obs ($\times 1000$)	Mean Income		Females	Age Shares %			Education Shares %			
		Males	Females	% Share	[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2005	283	31215	22935	44.1	47.9	37.5	14.6	10.9	35.7	29.9	23.6
2006	289	31945	23353	45.1	47.2	37.9	14.9	10.3	35.8	29.5	24.3
2007	292	33129	24397	46.1	46.4	38.5	15.1	9.9	35.3	29.5	25.4
2008	286	33606	25140	46.9	44.9	39.5	15.6	9.4	35.1	29.3	26.2
2009	281	32824	25411	47.3	43.1	40.6	16.3	9.1	35.2	29.0	26.7
2010	281	31682	24729	47.6	41.6	41.5	16.9	9.0	35.3	28.7	27.0
2011	279	30873	23991	48.0	39.8	42.7	17.4	8.8	35.0	28.5	27.6
2012	273	29345	22943	48.2	37.7	44.1	18.2	8.7	34.6	28.4	28.3
2013	273	28088	22382	48.0	36.0	45.2	18.9	8.9	34.7	27.9	28.5

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2005	2300	5677	8991	15835	22485	33471	48942	63131	104378	129582
2006	2456	6139	9537	16284	22988	33946	49398	63505	104070	129506
2007	2618	6690	10197	16898	23775	35213	51118	65830	108241	134470
2008	2711	6743	10203	17024	24324	36021	52166	66908	109279	135642
2009	2366	5591	9037	16407	24273	36148	52437	66492	109634	133683
2010	2263	5269	8505	15766	23617	35180	50875	64633	106835	129671
2011	2233	5160	8221	15245	23013	34199	49275	62837	103309	126178
2012	2000	4498	7399	14314	21961	32597	47140	60655	98747	121339
2013	1838	3881	6424	13116	21239	31951	46508	59414	95969	117924

Notes: LS sample, restricted to non-missing 1-year and 5-year changes in log earnings. Annual earnings are reported in 2018 U.S. dollars.

Table S-A3: Descriptive statistics for the H sample

(a) Panel A: Basic summary statistics

Year	Obs ($\times 1000$)	Mean Income		Females	Age Shares %			Education Shares %			
		Males	Females	% Share	[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2008	240	35505	27001	45.8	40.1	42.8	17.2	8.8	34.8	30.4	26.0
2009	242	34563	27082	46.5	38.7	43.6	17.7	8.6	34.7	30.0	26.7
2010	245	33390	26244	47.2	37.4	44.4	18.2	8.4	34.8	29.6	27.1
2011	244	32652	25483	47.7	35.6	45.5	18.9	8.2	34.5	29.5	27.8
2012	239	30914	24165	48.1	33.6	46.7	19.6	8.1	34.3	29.2	28.4
2013	238	30025	23815	48.1	31.9	47.8	20.3	8.0	34.2	28.9	28.9

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2008	3617	8556	12165	18571	25968	38213	54649	70024	113555	140634
2009	2844	7111	10741	17974	25788	38146	54522	69248	112818	137418
2010	2726	6648	10168	17382	25040	36971	52759	67078	109410	132854
2011	2724	6619	9948	16931	24430	35915	51096	65213	105915	129546
2012	2406	5840	9075	15974	23155	33922	48566	62297	100849	123337
2013	2217	5204	8317	15096	22628	33601	48233	61422	98156	121750

Notes: H sample, restricted to non-missing 1-year and 5-year changes in log earnings. Annual earnings are reported in 2018 U.S. dollars.

Table S-A4: Descriptive statistics for the B sample

(a) Panel A: Basic summary statistics

Year	Obs ($\times 1000$)	Mean Income	Age Shares %			Education Shares %			
		Males	[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2006	223.091	32112	41.0	34.5	24.6	17.7	40.0	26.5	15.8
2007	233.686	32131	40.3	34.6	25.1	17.3	40.0	26.3	16.3
2008	244.511	31391	40.0	34.7	25.3	17.3	40.1	26.0	16.6
2009	249.983	30035	38.9	35.1	26.0	17.0	40.0	25.9	17.0
2010	254.180	28484	37.7	35.5	26.8	16.8	40.2	25.7	17.3
2011	253.227	27125	36.2	36.1	27.7	16.5	40.5	25.5	17.6
2012	250.995	25070	34.4	36.9	28.7	16.3	40.6	25.3	17.8
2013	247.411	24227	32.4	37.6	29.9	16.2	40.7	25.2	17.9
2014	242.084	24497	30.6	38.3	31.1	16.1	40.7	25.0	18.2
2015	235.009	25784	29.1	38.7	32.2	15.8	40.8	24.9	18.5
2016	229.111	26906	27.7	39.1	33.2	15.4	40.9	24.8	18.9
2017	225.461	27476	26.8	39.0	34.2	15.0	40.8	24.8	19.4
2018	222.442	28281	26.4	38.7	35.0	14.7	40.7	24.8	19.7

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2006	0	6348	11950	18743	25032	37797	56784	74954	130901	168982
2007	0	3597	10834	18641	25187	38030	57152	75835	133075	170806
2008	0	1927	9019	18064	24881	37535	56419	74316	131104	166656
2009	0	0	6171	15999	24017	36692	55767	73403	129605	163291
2010	0	0	4756	13936	23024	35321	53682	70646	125337	159883
2011	0	0	2832	12210	22175	34055	51790	68500	121018	154562
2012	0	0	945	9812	20811	32009	48786	64957	113658	144361
2013	0	0	387	8207	19997	31455	48566	64027	110961	140965
2014	0	0	814	8556	20218	31774	48908	64455	112566	143896
2015	0	0	2016	10334	21073	32726	50304	66336	117219	150881
2016	0	0	3012	12294	21943	33682	51453	67728	120707	155770
2017	0	58	4333	13951	22307	33927	51268	67301	120179	154609
2018	0	824	5636	15252	22900	34367	51461	67515	120712	156436

Notes: B sample. Annual earnings are reported in 2018 U.S. dollars. Only males.

Table S-A5: Descriptive statistics for the B sample, with positive income

(a) Panel A: Basic summary statistics

Year	Obs ($\times 1000$)	Mean Income Males	Age Shares %			Education Shares %			
			[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2006	218.712	27711	40.9	34.5	24.6	17.6	40.0	26.6	15.8
2007	226.159	28087	40.2	34.7	25.1	17.1	40.2	26.4	16.4
2008	235.093	27620	39.8	34.8	25.4	17.0	40.2	26.1	16.7
2009	236.784	26826	38.4	35.3	26.3	16.5	40.1	26.1	17.3
2010	239.605	25564	37.2	35.7	27.1	16.3	40.4	25.8	17.6
2011	236.440	24577	35.6	36.2	28.2	15.8	40.6	25.7	17.9
2012	229.793	23167	33.5	36.8	29.6	15.4	40.5	25.8	18.3
2013	224.752	22563	31.6	37.5	30.9	15.1	40.7	25.7	18.5
2014	221.923	22607	30.1	38.2	31.7	15.2	40.8	25.4	18.7
2015	219.181	23388	28.7	38.8	32.4	15.0	40.9	25.2	18.9
2016	215.660	24183	27.5	39.2	33.2	14.7	40.9	25.1	19.2
2017	214.367	24448	26.7	39.1	34.2	14.5	40.8	25.1	19.6
2018	213.275	24954	26.3	38.8	34.9	14.2	40.7	25.1	20.0

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2006	1987	7403	11279	16162	21459	32301	48462	63857	111662	143935
2007	1644	7194	11285	16297	21779	32723	49028	64957	114061	145903
2008	1363	6242	10351	16010	21597	32416	48457	63754	112489	142797
2009	1047	5228	8377	14860	21097	31980	48220	63369	111545	140805
2010	1026	4402	6465	13631	20268	30855	46441	61151	107852	138024
2011	621	3280	5458	12701	19661	29917	45042	59569	104753	134212
2012	444	2664	5136	11486	18737	28388	42760	56862	99211	126801
2013	359	2335	4627	10309	18208	28116	42636	56154	97214	123367
2014	344	2184	4422	10157	18277	28228	42866	56400	98274	125706
2015	433	2466	4730	11140	18738	28809	43781	57660	101636	131751
2016	500	2852	5299	12401	19347	29465	44567	58613	104174	134866
2017	633	3445	6169	13222	19507	29513	44273	58038	103296	132568
2018	773	4052	7240	13949	19895	29760	44257	58048	103687	134422

Notes: B sample, positive income. Annual earnings are reported in 2018 euros. Only males.

Table S-A6: Descriptive statistics for the B sample, with positive income

(a) Panel A: Basic summary statistics

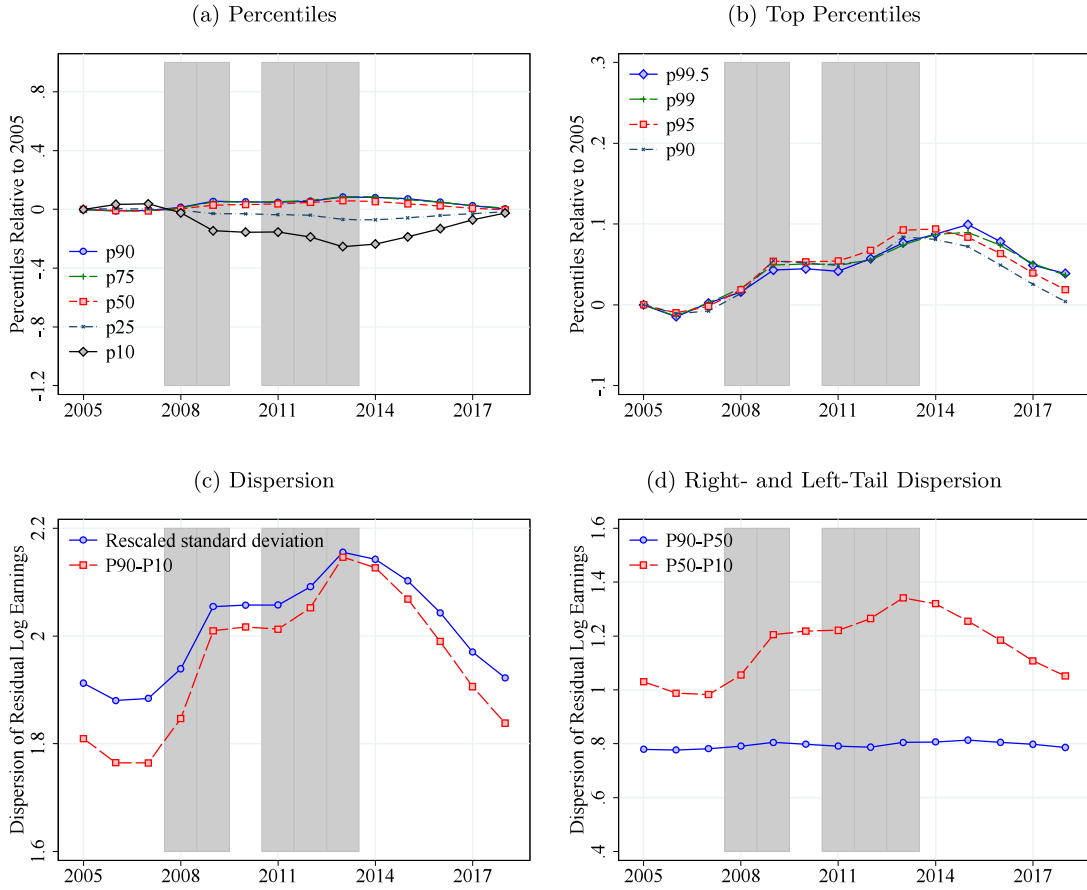
Year	Obs ($\times 1000$)	Mean Income	Age Shares %			Education Shares %			
		Males	[25,35]	[36,45]	[46,55]	Primary	Lower Sec	Upper Sec	College
2006	218.712	32755	40.9	34.5	24.6	17.6	40.0	26.6	15.8
2007	226.159	33200	40.2	34.7	25.1	17.1	40.2	26.4	16.4
2008	235.093	32648	39.8	34.8	25.4	17.0	40.2	26.1	16.7
2009	236.784	31709	38.4	35.3	26.3	16.5	40.1	26.1	17.3
2010	239.605	30217	37.2	35.7	27.1	16.3	40.4	25.8	17.6
2011	236.440	29051	35.6	36.2	28.2	15.8	40.6	25.7	17.9
2012	229.793	27384	33.5	36.8	29.6	15.4	40.5	25.8	18.3
2013	224.752	26670	31.6	37.5	30.9	15.1	40.7	25.7	18.5
2014	221.923	26723	30.1	38.2	31.7	15.2	40.8	25.4	18.7
2015	219.181	27646	28.7	38.8	32.4	15.0	40.9	25.2	18.9
2016	215.660	28585	27.5	39.2	33.2	14.7	40.9	25.1	19.2
2017	214.367	28898	26.7	39.1	34.2	14.5	40.8	25.1	19.6
2018	213.275	29496	26.3	38.8	34.9	14.2	40.7	25.1	20.0

(b) Panel B: Percentiles of annual earnings

Year	P1	P5	P10	P25	P50	P75	P90	P95	P99	P99.5
2006	2348	8750	13332	19104	25365	38181	57284	75481	131989	170135
2007	1944	8503	13339	19264	25743	38680	57953	76781	134824	172463
2008	1612	7378	12236	18924	25529	38316	57277	75359	132966	168791
2009	1238	6180	9902	17565	24937	37801	56998	74904	131850	166437
2010	1213	5203	7642	16112	23957	36472	54895	72283	127485	163148
2011	734	3877	6452	15013	23240	35363	53241	70412	123822	158644
2012	525	3149	6071	13576	22147	33555	50543	67213	117270	149883
2013	424	2760	5469	12186	21523	33234	50397	66376	114910	145824
2014	407	2582	5227	12006	21604	33366	50670	66667	116163	148589
2015	512	2914	5591	13168	22149	34053	51750	68155	120138	155734
2016	592	3371	6264	14658	22869	34829	52679	69282	123137	159416
2017	748	4072	7292	15629	23058	34886	52332	68602	122099	156700
2018	914	4790	8558	16488	23517	35177	52313	68614	122561	158891

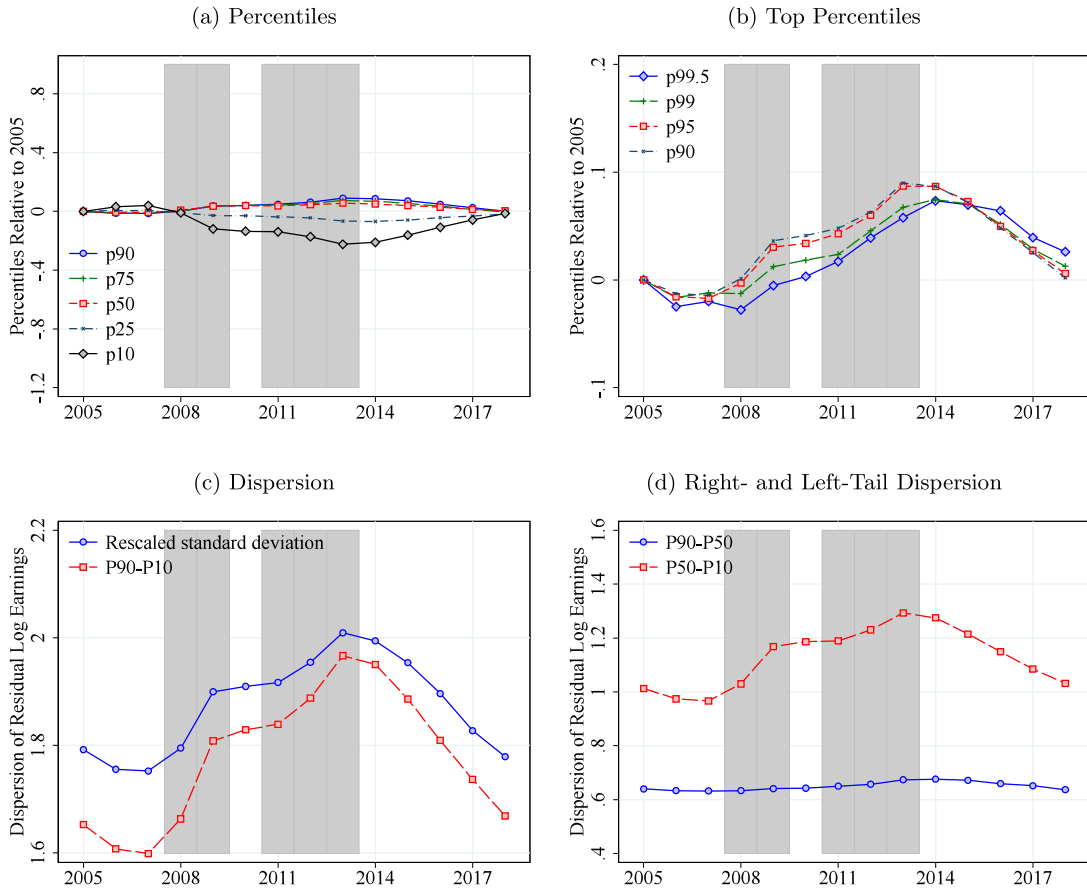
Notes: B sample, positive income. Annual earnings are reported in 2018 U.S. dollars. Only males.

Figure S-A1: Distribution of residual earnings in the population (males & females) after controlling for age



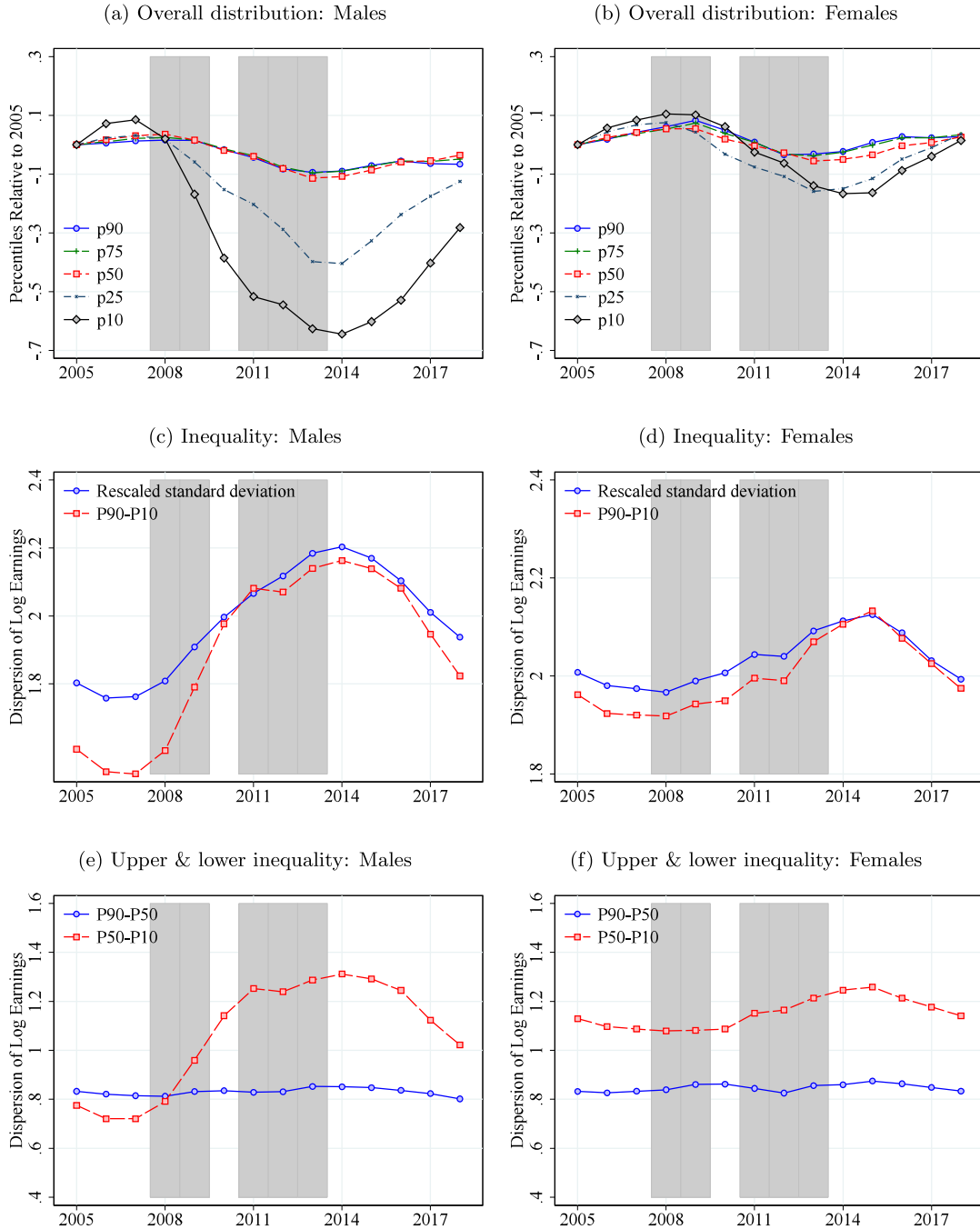
Notes: CS sample, percentiles of residualized log annual earnings, after controlling for age. All percentiles are normalized to 0 in 2005. The shaded areas indicate recession years.

Figure S-A2: Distribution of residual earnings in the population (males & females) after controlling for age and education



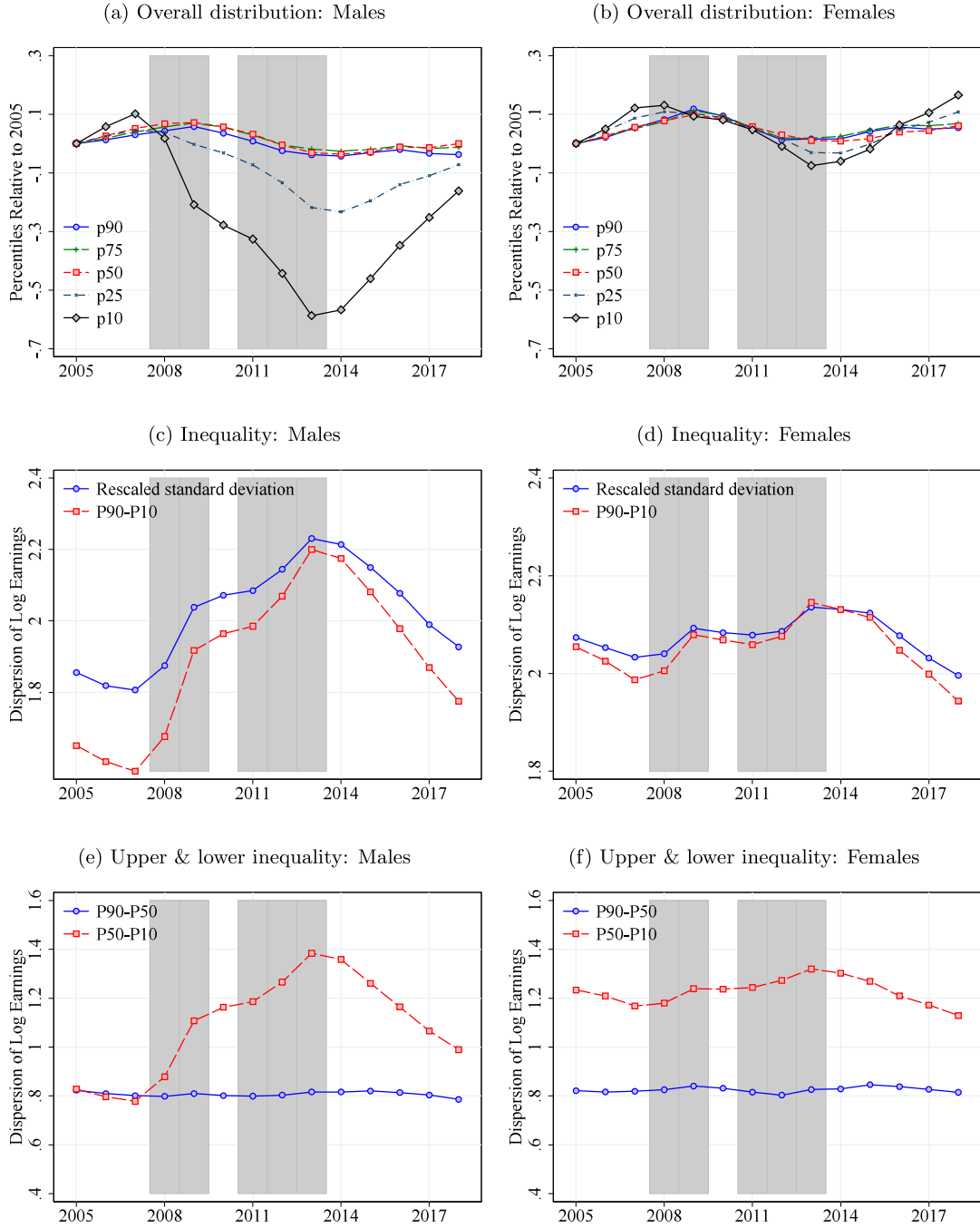
Notes: CS sample, percentiles of residualized log annual earnings, after controlling for age and education. All percentiles are normalized to 0 in 2005. The shaded areas indicate recession years.

Figure S-A3: Evolution of income percentiles and inequality, earnings & unemployment benefits



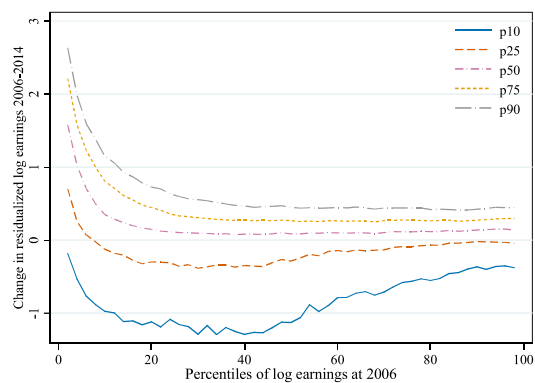
Notes: CS sample, earnings and unemployment benefits. Top panel: percentiles of log annual income, by gender. All percentiles are normalized to 0 in 2005. Middle and bottom panels: P90-P10 difference and rescaled standard deviation, and P90-P50 and P50-P10 percentiles differences. The shaded areas indicate recession years.

Figure S-A4: Evolution of earnings percentiles and inequality, no immigrants



Notes: CS sample, no immigrants. Top panel: percentiles of log annual earnings, by gender. All percentiles are normalized to 0 in 2005. Middle and bottom panels: P90-P10 difference and rescaled standard deviation, and P90-P50 and P50-P10 percentile differences. The shaded areas indicate recession years.

Figure S-A5: Log earnings changes between 2006 and 2014 against initial earnings



Notes: Non-missing observations on residualized log earnings in 2006 and 2014. On the x-axis we report percentiles of log earnings in 2006. On the y-axis we report the changes in residualized log earnings between 2006 and 2014.

S-B The welfare cost of income risk

Consider an individual with utility function $U_i(C_{it}) = \frac{(C_{it}-C_m)^{1-\theta_i}-1}{1-\theta_i}$, with consumption $C_{it} = \lambda(X_{it})Y_{it}$ for some proportionality factor $\lambda(X_{it})$. Suppose that

$$\ln(C_{it} - C_m) | X_{it} = x \sim \mathcal{N}(\mu(x), \sigma(x)^2).$$

The individual is willing to give up $a\%$ of consumption each period in order to eliminate income risk, where a solves

$$U_i(\mathbb{E}(C_{it} | X_{it})(1-a)) = \mathbb{E}[U_i(C_{it}) | X_{it}].$$

Equivalently, omitting the dependence on X_{it} for simplicity, a solves

$$\begin{aligned} \left(\left(C_m + \exp\left(\mu + \frac{1}{2}\sigma^2\right) \right) (1-a) - C_m \right)^{1-\theta_i} &= \mathbb{E} \left[(C_{it} - C_m)^{1-\theta_i} \right] \\ &= \exp \left[(1-\theta_i)\mu + \frac{1}{2}(1-\theta_i)^2\sigma^2 \right]. \end{aligned}$$

It follows that

$$a = 1 - \frac{C_m + \exp\left[\mu + \frac{1}{2}(1-\theta_i)\sigma^2\right]}{C_m + \exp\left(\mu + \frac{1}{2}\sigma^2\right)}.$$

Hence, for small σ ,

$$a = \frac{1}{2}\theta_i \frac{\exp(\mu)}{C_m + \exp(\mu)}\sigma^2 + o(\sigma^2).$$

Now, we have

$$\text{CV} = \sqrt{\frac{2}{\pi}} \frac{\exp(\mu)}{C_m + \exp(\mu)}\sigma + o(\sigma).$$

Hence

$$a = \frac{\pi}{4}\theta_i \frac{C_m + \exp(\mu)}{\exp(\mu)}\text{CV}^2 + o(\sigma^2).$$

This implies (3), and (2) in the special case where $C_m = 0$.

S-C Poisson regression results

Table S-C1: Poisson regression results

	(1)	(2)
	Income levels	Income absolute deviations
Log lagged income	0.525 (0.107)	1.025 (0.257)
Log lagged income squared	0.532 (0.0864)	-0.0107 (0.203)
Log lagged income cubed	0.0299 (0.0291)	-0.0251 (0.0771)
Indicator that lagged income is zero	-4.798 (2.557)	2.732 (4.829)
Age	-0.0666 (0.00875)	-0.0251 (0.0317)
Age squared	0.000615 (0.000102)	-0.000444 (0.00039)
Education: lower secondary	0.102 (0.0183)	-0.0280 (0.0905)
Education: upper secondary	0.315 (0.0204)	0.347 (0.0955)
Education: college	0.733 (0.0257)	0.859 (0.146)
Days worked in past year	-0.00134 (0.000315)	-0.00382 (0.000978)
Indicator that out-of-work income is zero	-1.409 (0.181)	-2.475 (0.631)
Log out-of-work income in past year	-0.997 (0.0917)	-1.393 (0.321)
Indicator that worked full year in past year	-0.0214 (0.0416)	0.0136 (0.201)
Indicator that worked full year in past two years	0.00279 (0.0343)	-0.414 (0.221)
Indicator that worked full year in past three years	0.0797 (0.0242)	0.536 (0.262)
Permanent contract in past year	-0.0149 (0.0236)	0.173 (0.138)
Full-time contract in past year	0.219 (0.0359)	0.225 (0.159)
Intercept	11.11 (0.185)	11.08 (0.657)
<i>N</i>	3111191	3111191

Notes: *B* sample. Robust standard errors in parentheses, clustered at the individual level. In column (2), the dependent variable is $|Y_{it} - \exp(X'_{it}\hat{\beta})|$, where $\hat{\beta}$ is shown in column (1). The standard errors in column (2) are computed using a cluster bootstrap with 100 repetitions to account for the fact that $\hat{\beta}$ is estimated. Macro predictors and interactions with age and age squared are included in the regressions, but omitted from the table for conciseness.

S-D Unobserved heterogeneity: a grouped fixed-effects approach

In this section we describe how we allow for unobserved predictors. To implement the grouped fixed-effects approach of [Bonhomme et al. \(2022\)](#), one possibility would be to group individuals based on their mean income. However, in an unbalanced panel this approach tends to mix individual-specific heterogeneity and age, particularly when there is a strong life-cycle component to income. To account for age, we proceed in two steps.

In the first step, we maximize the Poisson log likelihood

$$\sum_{i,t} \left[Y_{it} \tilde{X}_{it}' \beta(k_i) - \exp(\tilde{X}_{it}' \beta(k_i)) \right], \quad (\text{S-D6})$$

with respect to parameters $\beta(k)$ and group indicators k_i , where $\tilde{X}_{it} = (1, \text{age}_{it}, \text{age}_{it}^2)'$. To implement the minimization, we use a Lloyd-like algorithm (see [Bonhomme and Manresa, 2015](#)). We start with 20 randomly chosen parameter values, and select the solution that corresponds to the highest value of the objective function. Given each starting value, we stop the algorithm when the change in the log likelihood is less than 10^{-10} . This first step gives us parameters $\tilde{\beta}(k)$ and group indicators \tilde{k}_i .

In the second step, we include all our macro and micro predictors X_{it} . We aim to maximize

$$\sum_{i,t} \left[Y_{it} X_{it}' \beta(k_i) - \exp(X_{it}' \beta(k_i)) \right], \quad (\text{S-D7})$$

again with respect to parameters $\beta(k)$ and group indicators k_i . In this specification, we account for group effects in the intercept and the coefficients of age and age squared. We use 10 iterations of a Lloyd-like algorithm. The group indicators \tilde{k}_i provide a starting value to initiate the algorithm. This second step gives us parameters $\hat{\beta}(k)$ and group indicators \hat{k}_i , which are the ones we use to construct our prediction $\exp(X_{it}' \hat{\beta}(\hat{k}_i))$, which is the denominator of CV. We proceed similarly for the numerator. Hence, the CV coefficient is constructed using two sets of groups.

We apply the method to the B sample, restricted to individuals with at least 4 observations, using 4 groups for both the numerator and the denominator of CV. In [Online Appendix Figure S-D1](#) we show the income profiles by age for the estimated clusters that we obtain

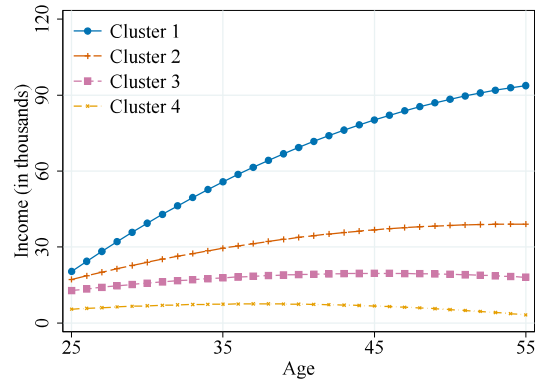
Table S-D1: Education Distribution of Individuals by Cluster

(a) Mean clusters					
Cluster	# of Indiv.	Education (Proportion of Indivs.)			
		Primary	Lower Sec.	Upper Sec.	College
1	20002	0.16	0.33	0.27	0.24
2	96641	0.17	0.39	0.25	0.19
3	132677	0.16	0.43	0.25	0.16
4	56827	0.23	0.40	0.23	0.14

(b) Absolute deviation clusters					
Cluster	# of Indiv.	Education (Proportion of Indivs.)			
		Primary	Lower Sec.	Upper Sec.	College
1	73778	0.17	0.43	0.24	0.17
2	100890	0.17	0.39	0.25	0.19
3	51268	0.20	0.42	0.23	0.15
4	80211	0.17	0.39	0.27	0.17

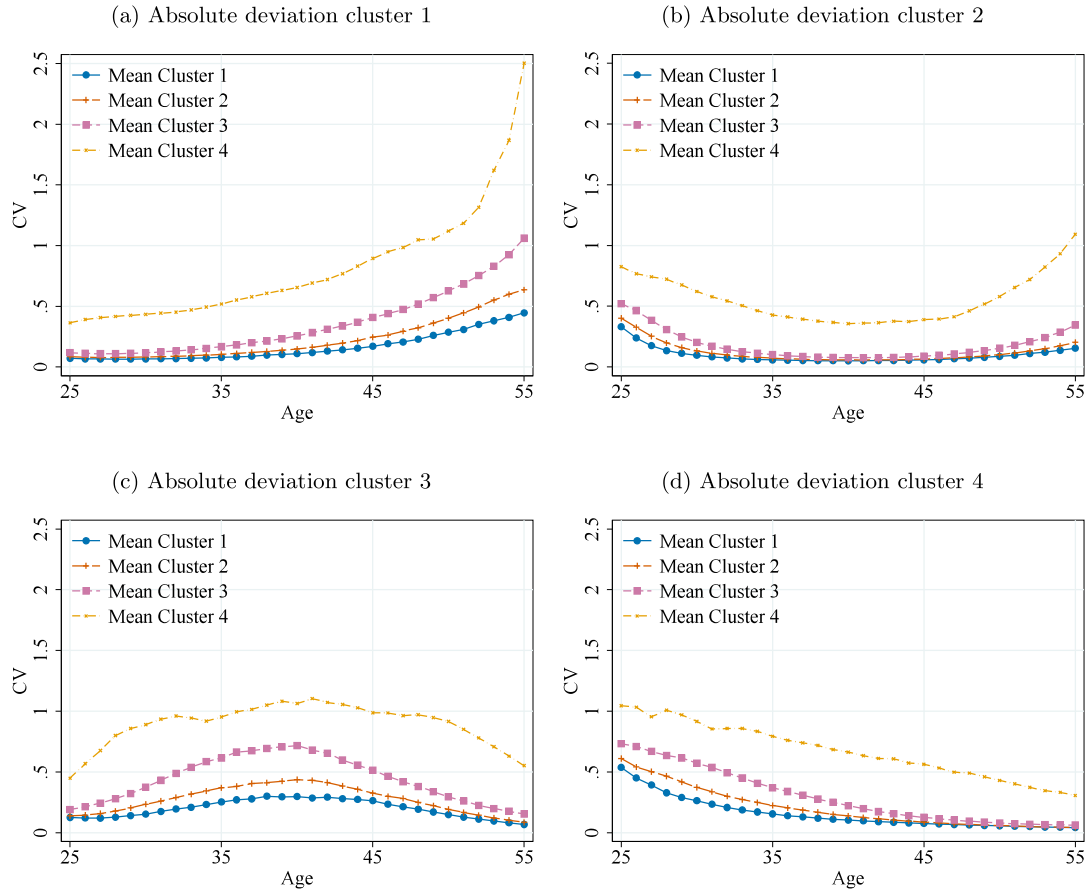
Notes: *B* sample, individuals with at least 4 observations prior to 2018. Specification with unobserved heterogeneity, 4 groups. The mean clusters correspond to the prediction of income levels, the absolute deviation clusters correspond to the prediction of income absolute deviations.

Figure S-D1: Predicted age income profiles for the estimated mean groups ($K = 4$)



Notes: *B* sample, individuals with at least 4 observations prior to 2018. Specification with unobserved heterogeneity, 4 groups. The mean clusters correspond to the prediction of income levels, the absolute deviation clusters correspond to the prediction of income absolute deviations.

Figure S-D2: Average CV over age, by mean cluster and absolute deviation cluster



Notes: B sample, individuals with at least 4 observations prior to 2018. Specification with unobserved heterogeneity, 4 groups. The mean clusters correspond to the prediction of income levels, the absolute deviation clusters correspond to the prediction of income absolute deviations.

using the above algorithm to predict income levels (the “mean clusters”). The clusters differ not only in the level of income, but also in the curvature of the profiles. In Online Appendix Figure S-D2 we show the CV profiles by age for all combinations of the mean clusters and the clusters that we obtain when predicting income absolute deviations (the “absolute deviation clusters”). We see that, while the former tends to capture differences in risk levels between individuals, the latter tends to pick up differences in age profiles. Lastly, in Online Appendix Table S-D1 we show the number of individuals in each cluster and the corresponding distribution of educational attainment. We find that the mean clusters are correlated with education, consistently with the fact that the higher educated tend to face lower risk levels. In contrast, the absolute deviation clusters are virtually independent of education.

S-E Enforcing non-negativity of outcomes in quantile regression

Let $Y \mid X$ be a non-negative random variable with quantile function $g(x, \tau)$. In our application, Y is income or income absolute deviation, and X includes our micro and macro predictors. Let $\Pr(Y = 0 \mid X = x) = \pi(x)$. Thus, $g(x, \tau) = 0$ for $\tau \leq \pi(x)$. Also,

$$\Pr(Y \leq g(x, \tau) \mid Y > 0, \tau > \pi(x), X = x) = \frac{\tau - \pi(x)}{1 - \pi(x)}.$$

Denote the s -conditional quantile of Y given $Y > 0, X = x$ by $Q_s(Y \mid Y > 0, X = x) = \psi(x, s)$ so that

$$g(x, \tau) = \begin{cases} 0 & \text{for } \tau \leq \pi(x) \\ \psi\left(x, \frac{\tau - \pi(x)}{1 - \pi(x)}\right) & \text{for } \tau > \pi(x) \end{cases}.$$

For $\pi(x) \approx 0$, we have $g(x, \tau) \approx \psi(x, \tau)$.

An estimator of $g(x, \tau)$ that enforces non-negativity is as follows. First, we obtain the estimates $\hat{\psi}(x, s) = \exp[\hat{\gamma}(s)' \varphi(x)]$, and, using logit, $\hat{\pi}(x) = \Lambda[\hat{\beta}' \varphi(x)]$ where $\Lambda(v) = \exp(v)/(1 + \exp(v))$. To get $\hat{\gamma}(s)$, we run linear quantile regressions of log income on $\varphi(x)$ in the subsample with positive income; $\hat{\beta}$ is a logit estimate; and $\varphi(x)$ is a vector of functions of x . Finally, we compute:

$$\hat{g}(x, \tau) = \begin{cases} 0 & \text{for } \tau \leq \hat{\pi}(x) \\ \hat{\psi}\left(x, \frac{\tau - \hat{\pi}(x)}{1 - \hat{\pi}(x)}\right) & \text{for } \tau > \hat{\pi}(x) \end{cases}.$$

To ease the computational burden, we model $\gamma(s)$ as piecewise linear interpolating splines on a grid, $[\tau_1, \tau_2], [\tau_2, \tau_3], \dots, [\tau_{L-1}, \tau_L]$, contained in the unit interval. The intercept coefficients on $(0, \tau_1]$ and $[\tau_L, 1)$ are parameterized as the quantiles of an exponential distribution on their respective supports. In practice, we use an equally spaced grid on the unit interval with $L = 11$.

S-F Estimating measures of location and dispersion from subjective probabilistic income expectations

For each respondent in the Spanish Survey of Household Finances (EFF) who answers the subjective probabilistic income expectations question described in Section 6, we observe the fraction of points \hat{p}_j allocated to each event $j = 1, \dots, 5$ (adding up to 1). Here we present a simple approach to calculate summary measures of location and dispersion from these observations under the assumption that the underlying probabilities are normally distributed (with mean μ and standard deviation σ). That is, we assume that the underlying process for next year's log income is a random walk with a household-specific drift μ_i and normally distributed shocks with a household-specific standard deviation σ_i . The household index is omitted in the text for conciseness.

Under normality, $p_1 = \Phi(-0.1\beta - \alpha)$, $p_2 = \Phi(-0.02\beta - \alpha) - \Phi(-0.1\beta - \alpha)$, $p_3 = \Phi(0.02\beta - \alpha) - \Phi(-0.02\beta - \alpha)$, $p_4 = \Phi(0.1\beta - \alpha) - \Phi(0.02\beta - \alpha)$, $p_5 = 1 - \Phi(0.1\beta - \alpha)$, for $\alpha = \mu/\sigma$ and $\beta = 1/\sigma$. Elicited probabilities \hat{p}_j can be regarded as noisy measurements of p_j due to rounding and the inherent randomness in the elicitation process. If the \hat{p}_j are regarded as sample frequencies from a hypothetical random sample of size m , they are the unrestricted maximum likelihood estimates of the p_j from the multinomial log likelihood:

$$L(p) = \sum_j m \hat{p}_j \log p_j.$$

Alternatively, $p = (p_1, \dots, p_4)$ can be estimated as the posterior mean of a posterior distribution proportional to $\exp[L(p) + \log \pi(p)]$, for some chosen prior $\pi(p)$ and value of m (e.g., $m = 10$). A conventional option is to use Jeffreys prior, $\log \pi(p) = -\frac{1}{2} \sum_{j=1}^5 \log p_j + C$, for some normalizing constant C . This is a Dirichlet distribution of order $J = 5$, which is the conjugate prior of the multinomial, therefore the posterior is also Dirichlet with posterior

means given by:

$$\tilde{p}_j = \frac{\hat{p}_j + \frac{1}{2m}}{1 + \frac{J}{2m}}.$$

Jeffreys prior adds $J/2$ observations to the likelihood with equally distributed probabilities. The modified estimator \tilde{p}_j has the advantage that it takes values in the open interval $(0, 1)$ so that the inverse normal cdf transformation is still defined when $\hat{p}_j = 0$ or 1 . In the present statistical framework, m measures the accuracy of the process of eliciting subjective probabilities.

We implement this approach, using a Berkson estimator that enforces the Gaussian restrictions on the posterior means \tilde{p}_j . This estimator is based on the inverse normal probabilities:

$$\begin{aligned} q_1 &= \Phi^{-1}(1 - c_1) = 0.1\beta + \alpha \\ q_2 &= \Phi^{-1}(1 - c_2) = 0.02\beta + \alpha \\ q_3 &= \Phi^{-1}(1 - c_3) = -0.02\beta + \alpha \\ q_4 &= \Phi^{-1}(1 - c_4) = -0.1\beta + \alpha \end{aligned}$$

where the c_j are the cumulative probabilities $c_j = \sum_{k=1}^j p_k$. Sample counterparts are

$$\tilde{c}_j = \sum_{k=1}^j \tilde{p}_k = \frac{\hat{c}_j + \frac{j}{2m}}{1 + \frac{J}{2m}}$$

and $\tilde{q}_j = \Phi^{-1}(1 - \tilde{c}_j)$. To estimate μ and σ we choose a particular solution of the previous system with an intuitive interpretation:

$$\begin{aligned} \tilde{\mu} &= \frac{1}{2} \times \frac{(\tilde{q}_1 + \tilde{q}_4) + (\tilde{q}_2 + \tilde{q}_3)}{5(\tilde{q}_1 - \tilde{q}_4) + 25(\tilde{q}_2 - \tilde{q}_3)}, \\ \tilde{\sigma} &= \frac{2}{5(\tilde{q}_1 - \tilde{q}_4) + 25(\tilde{q}_2 - \tilde{q}_3)}. \end{aligned}$$

Lastly, mimicking the fact that the maximum likelihood estimator of $\theta = (\alpha, \beta)$ is $\hat{\theta} = \arg \max_{\theta} \sum_j \hat{p}_j \ln p_j(\theta)$, an alternative method to enforce the restrictions on the posterior means \tilde{p}_j would be to compute

$$\tilde{\theta} = \arg \max_{\theta} \sum_j \tilde{p}_j \ln p_j(\theta).$$

Nevertheless, in our empirical calculations of subjective risks we relied on the Berkson estimator, which has a simple closed-form expression.

S-G Additional tables and figures on robustness checks

S-G.1 After-tax income

Table S-G1: Effective Tax Rates

year	base_1	tau_1	base_2	tau_2	base_3	tau_3	base_4	tau_4	base_5	tau_5	base_6	tau_6
2005	0	8.72	4080.0	4.42	14076.0	10.28	26316.0	16.74	45900.0	26.43	.	.
2006	0	11.29	4161.6	4.71	14357.5	10.52	26842.3	17.03	46818.0	26.89	.	.
2007	0	5.68	17360.0	12.32	32360.0	18.49	52360.0	27.5
2008	0	3.68	17707.2	10.51	33007.2	17.38	53407.2	26.83
2009	0	3.31	17707.2	10.45	33007.2	17.28	53407.2	26.66
2010	0	4.17	17707.2	12.25	33007.2	18.34	53407.2	27.03
2011	0	3.74	17707.2	12.21	33007.2	18.25	53407.2	26.42	120000.2	34.59	175000.2	39.58
2012	0	3.75	17707.2	12.93	33007.2	19.47	53407.2	28.28	120000.2	37.61	175000.2	43.31
2013	0	3.62	17707.2	13.12	33007.2	19.55	53407.2	28.32	120000.2	37.75	175000.2	43.80
2014	0	3.48	17707.2	13.12	33007.2	19.52	53407.2	28.16	120000.2	37.52	175000.2	43.68
2015	0	1.68	12450.0	5.95	20200.0	12.66	34000.0	18.81	60000.0	28.68	.	.
2016	0	2.04	12450.0	6.02	20200.0	12.89	35200.0	19.22	60000.0	28.62	.	.
2017	0	2.47	12450.0	6.20	20200.0	12.79	35200.0	19.38	60000.0	28.92	.	.
2018	0	2.47	12450.0	6.20	20200.0	12.79	35200.0	19.38	60000.0	28.92	.	.

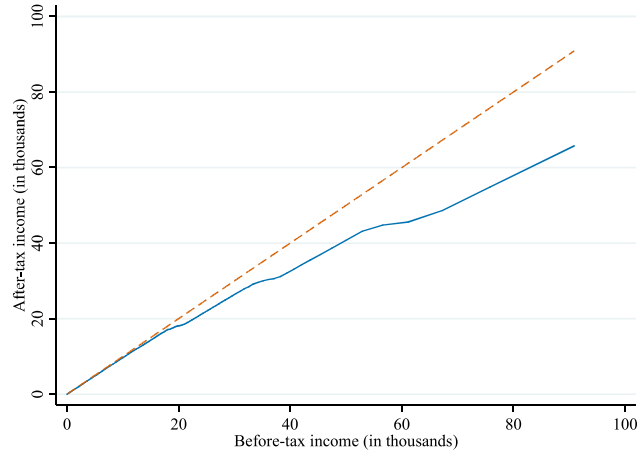
Notes: “base_x” represents the upper and lower bounds of income brackets. “tau_x” represents the average effective tax rates. All income bracket bounds are in nominal euros. Average effective tax rates are in percent.

Table S-G2: Income risk over the period, in numbers, after-tax income

	All	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
P90/P10	9.17	5.18	5.65	5.72	6.76	9.16	9.89	10.95	12.68	13.32	11.91	10.37	9.31	8.25
P90/P50	6.41	3.97	4.20	4.19	4.92	6.41	6.70	7.23	8.17	8.46	7.75	6.93	6.52	5.81
P50/P10	1.43	1.30	1.34	1.36	1.37	1.43	1.48	1.51	1.55	1.58	1.54	1.50	1.43	1.42
p10	0.07	0.08	0.08	0.08	0.08	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.08	0.07
p25	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08	0.08
p50	0.11	0.10	0.10	0.10	0.11	0.10	0.10	0.11	0.11	0.11	0.11	0.11	0.11	0.10
p75	0.32	0.23	0.24	0.24	0.27	0.34	0.36	0.40	0.45	0.46	0.42	0.35	0.33	0.29
p90	0.67	0.40	0.43	0.43	0.52	0.67	0.70	0.80	0.90	0.93	0.85	0.75	0.70	0.61

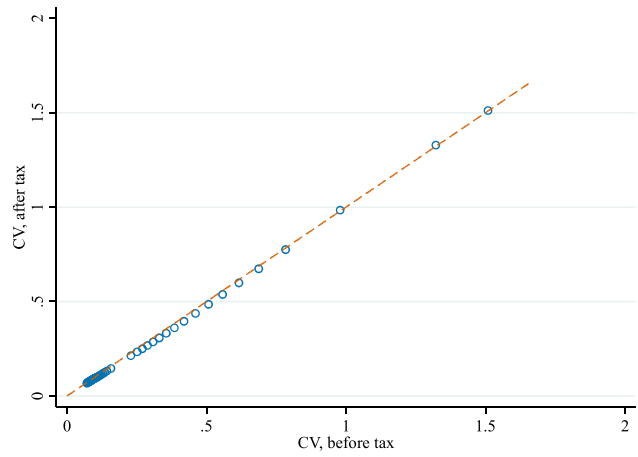
Notes: B sample. Exponential specification, using all macro and micro predictors. After-tax income.

Figure S-G1: Before-tax and after-tax income



Notes: Income in thousands of euros. See the text for how we construct after-tax income.

Figure S-G2: Quantile-quantile plot of before-tax and after-tax CV



Notes: B sample. On the x-axis we report the percentiles of CV based on before-tax income. On the y-axis we report the percentiles of CV based on after-tax income.

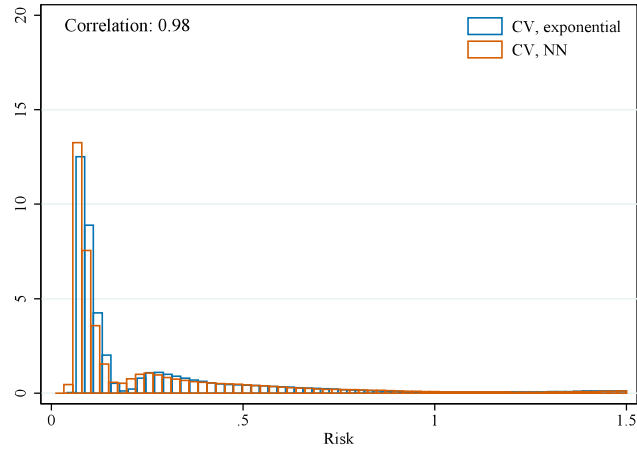
S-G.2 Neural network specification

Table S-G3: Income risk over the period, in numbers, neural network specification

	All	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
P90/P10	10.82	6.41	6.96	7.04	7.85	9.33	10.52	12.51	14.16	14.93	13.98	12.59	11.43	10.63
P90/P50	6.63	4.31	4.64	4.69	5.27	6.03	6.55	7.55	8.09	8.07	7.66	7.10	6.76	6.49
P50/P10	1.63	1.49	1.50	1.50	1.49	1.55	1.61	1.66	1.75	1.85	1.83	1.77	1.69	1.64
p10	0.07	0.07	0.06	0.07	0.07	0.07	0.07	0.07	0.06	0.06	0.06	0.06	0.07	0.06
p25	0.08	0.08	0.07	0.08	0.08	0.08	0.08	0.07	0.07	0.07	0.07	0.07	0.08	0.07
p50	0.11	0.10	0.10	0.10	0.11	0.11	0.11	0.11	0.11	0.12	0.11	0.11	0.12	0.10
p75	0.34	0.23	0.22	0.24	0.30	0.38	0.40	0.42	0.45	0.49	0.46	0.37	0.37	0.28
p90	0.71	0.45	0.45	0.47	0.58	0.66	0.71	0.81	0.87	0.94	0.87	0.78	0.81	0.64

Notes: B sample. Neural network specification with Poisson loss. One layer with 8 nodes for the conditional mean and 7 nodes for the conditional mean absolute deviation.

Figure S-G3: Two specifications of CV, exponential and neural network



Notes: B sample, using all macro and micro predictors. The correlation coefficient is computed after trimming the 99th percentiles of both CV measures.

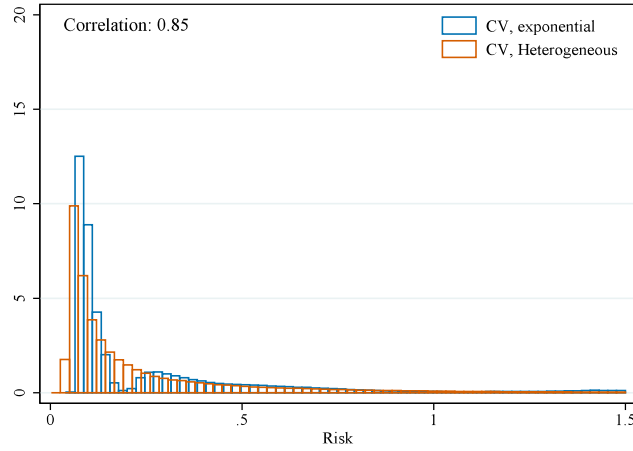
S-G.3 Specification with unobserved heterogeneity

Table S-G4: Income risk over the period, in numbers, specification with unobserved heterogeneity

	All	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
P90/P10	10.59	6.48	6.86	7.41	8.73	10.72	11.25	12.09	13.29	13.72	12.97	11.76	10.86	9.60
P90/P50	5.00	3.35	3.56	3.83	4.35	4.98	5.03	5.28	5.56	5.69	5.70	5.46	5.27	4.74
P50/P10	2.12	1.93	1.93	1.94	2.01	2.15	2.24	2.29	2.39	2.41	2.28	2.15	2.06	2.03
p10	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.06	0.05	0.05	0.05
p25	0.07	0.08	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07
p50	0.12	0.12	0.11	0.11	0.11	0.12	0.12	0.13	0.14	0.14	0.13	0.12	0.11	0.11
p75	0.27	0.21	0.21	0.21	0.24	0.28	0.31	0.34	0.37	0.37	0.33	0.28	0.25	0.23
p90	0.60	0.39	0.40	0.42	0.50	0.59	0.63	0.71	0.77	0.78	0.73	0.64	0.60	0.53

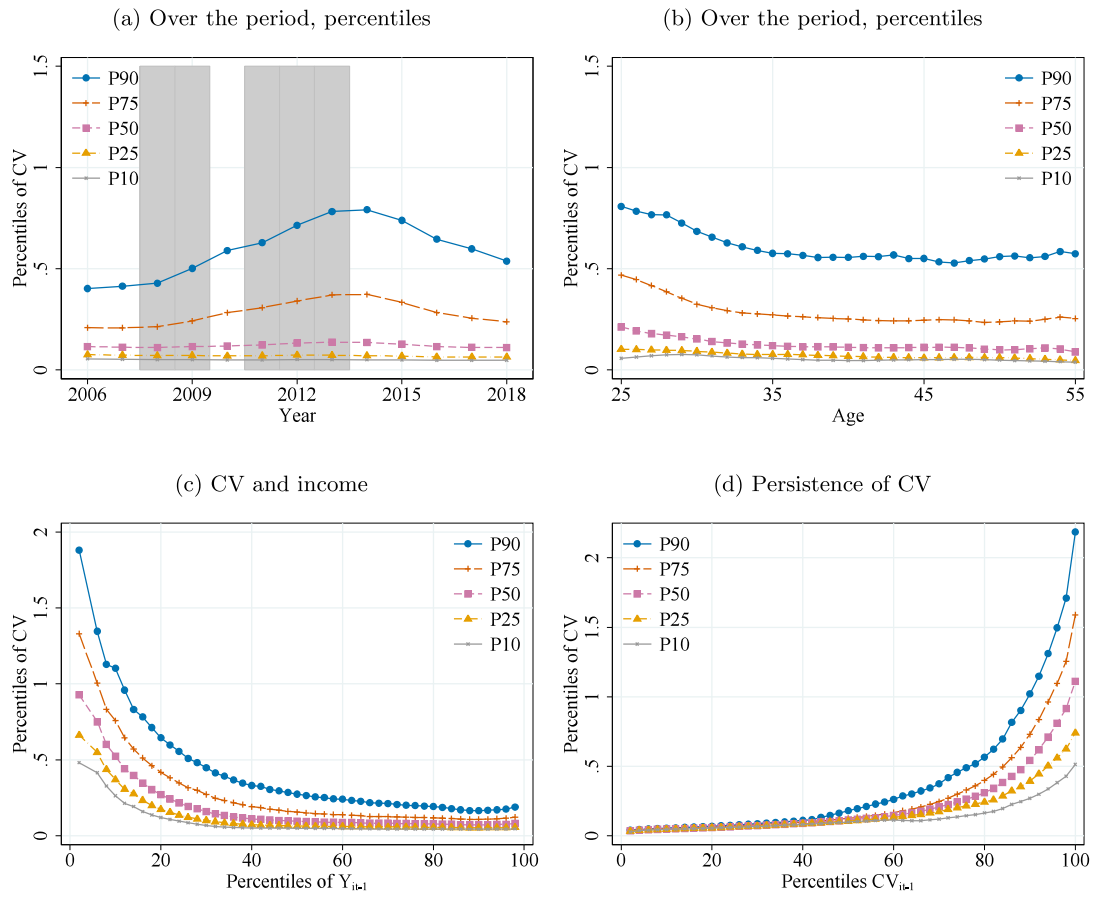
Notes: B sample, individuals with at least 4 observations prior to 2018. Exponential specification, using all macro and micro predictors and unobserved heterogeneity. 4 groups.

Figure S-G4: Two specifications of CV, with and without unobserved heterogeneity



Notes: B sample, individuals with at least 4 observations prior to 2018. Exponential specification, using all macro and micro predictors, and unobserved heterogeneity in the right graph (4 groups). The correlation coefficient is computed after trimming the 99th percentiles of both CV measures.

Figure S-G5: CV, specification with unobserved heterogeneity, 6 groups



Notes: *B* sample, individuals with at least 4 observations prior to 2018. Exponential specification, using all macro and micro predictors, and unobserved heterogeneity. 6 groups.

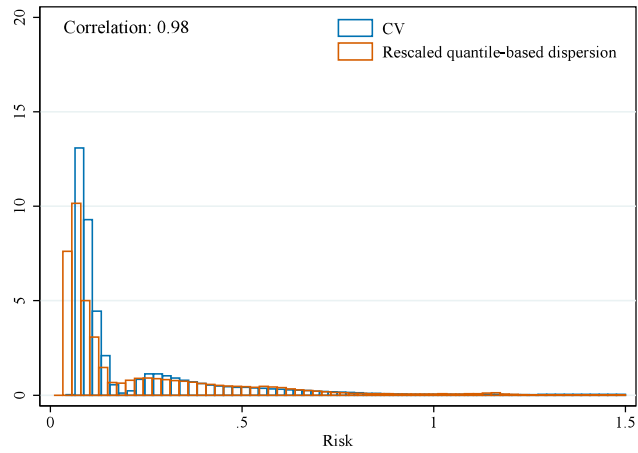
Table S-G5: Income risk over the period, in numbers, specification with unobserved heterogeneity, 6 groups

	All	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
P90/P10	11.99	7.33	7.81	8.34	9.76	11.90	12.62	13.77	15.23	15.75	14.94	13.65	12.64	11.28
P90/P50	5.04	3.47	3.68	3.87	4.34	4.99	5.09	5.36	5.70	5.83	5.80	5.57	5.36	4.87
P50/P10	2.38	2.11	2.12	2.16	2.25	2.39	2.48	2.57	2.67	2.70	2.58	2.45	2.36	2.32
p10	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05	0.05
p25	0.07	0.08	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.07	0.06	0.06	0.06
p50	0.12	0.12	0.11	0.11	0.12	0.12	0.12	0.13	0.14	0.14	0.13	0.12	0.11	0.11
p75	0.27	0.21	0.21	0.21	0.24	0.28	0.31	0.34	0.37	0.37	0.33	0.28	0.26	0.24
p90	0.60	0.40	0.41	0.43	0.50	0.59	0.63	0.71	0.78	0.79	0.74	0.65	0.60	0.54

Notes: B sample, individuals with at least 4 observations prior to 2018. Exponential specification, using all macro and micro predictors and unobserved heterogeneity. 6 groups.

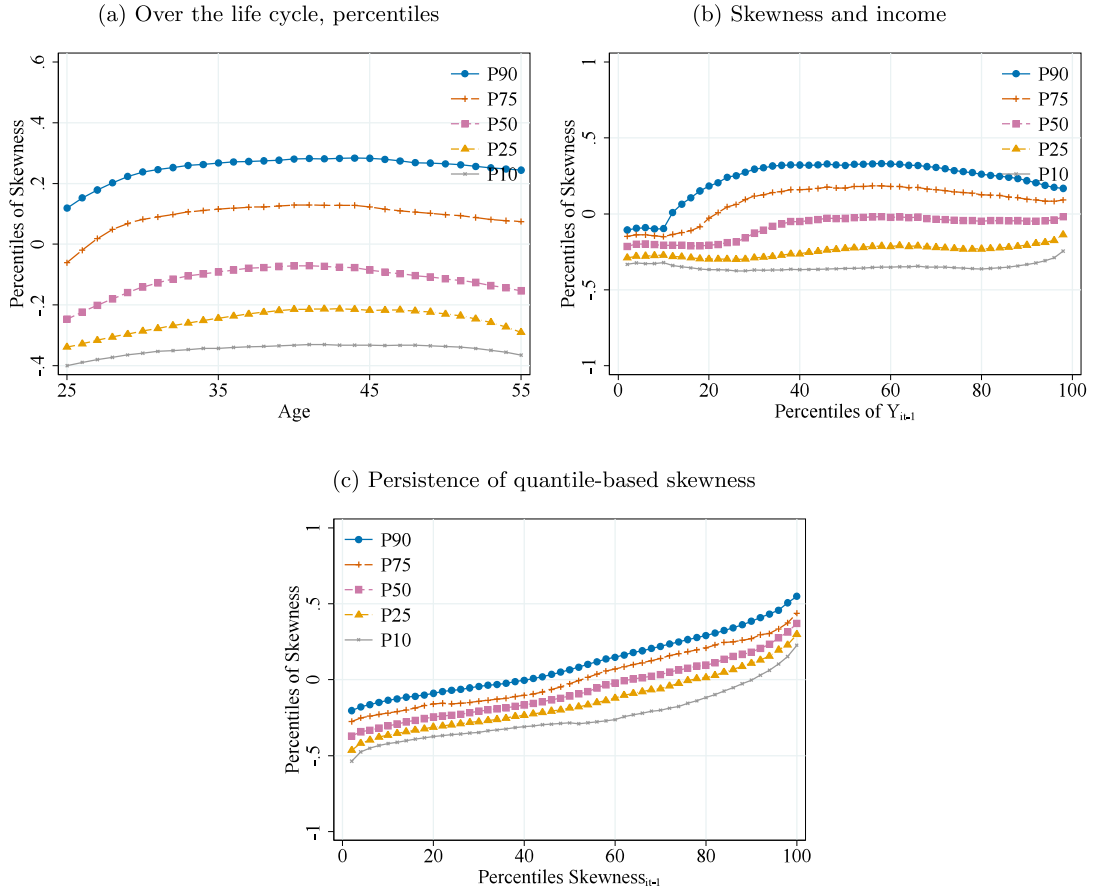
S-G.4 Beyond the CV

Figure S-G6: Comparing CV and quantile-based dispersion



Notes: B sample, with positive income. CV is our CV measure (i.e., conditional mean absolute deviation divided by conditional mean). Quantile-based dispersion is $P90(X_{it}) - P10(X_{it})$ (rescaled), where $P90(X_{it})$ and $P10(X_{it})$ are estimated using linear quantile regressions of log income on all macro and micro predictors. The correlation coefficient is computed after trimming the 99th percentiles of both CV measures.

Figure S-G7: Quantile-based skewness, additional results



Notes: *B* sample, with positive income. Quantile-based measure of skewness risk, $\frac{P90(X_{it}) - 2P50(X_{it}) + P10(X_{it})}{P90(X_{it}) - P10(X_{it})}$, where $P90(X_{it})$, $P50(X_{it})$, and $P10(X_{it})$ are estimated using linear quantile regressions of log income on all macro and micro predictors.

References

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